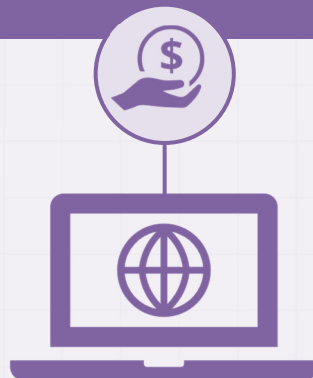


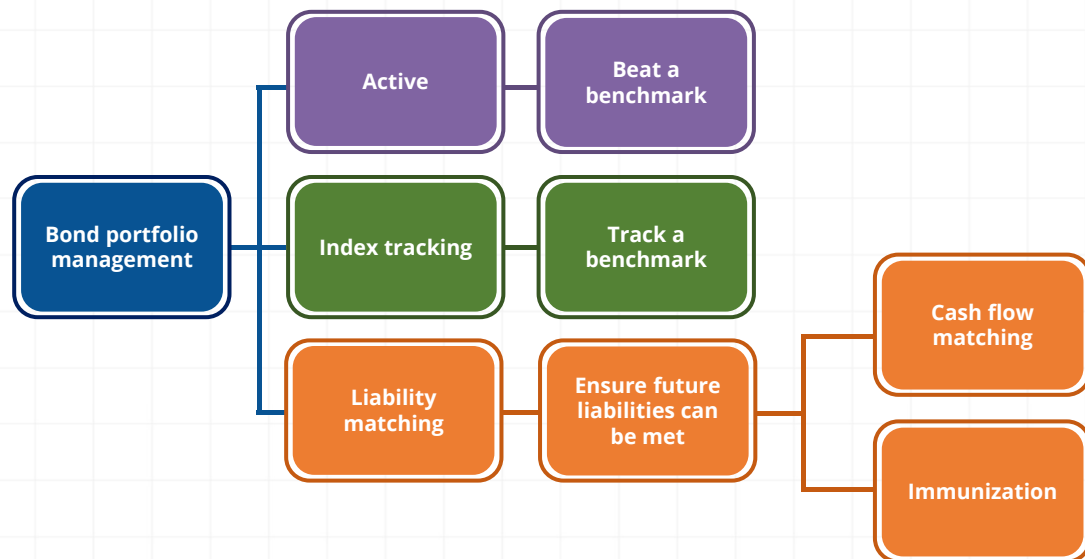


Fixed Income Portfolio Management Techniques

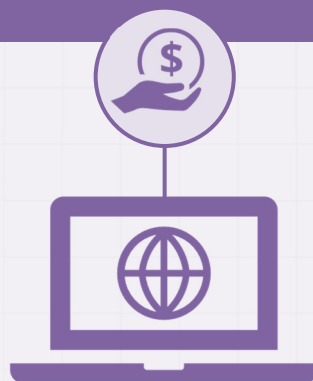
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Fixed Income Portfolio Management Techniques

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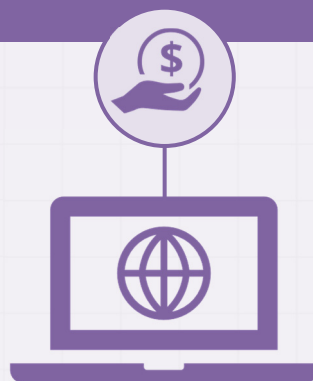
Bond Portfolio Risk

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	Interest rate risk	Risk of reduction in portfolio value if interest rates increase
	Reinvestment risk	Risk of reduction in returns on reinvested cash flows if interest rates decrease
	Credit risk	Risk of borrower not making scheduled interest or capital repayments, or reduction in bond value if risk of default increases
	Inflation risk	Risk of reduction of real returns on fixed income products if inflation is higher than expected
	FX risk	Risk of depreciation of FX rate in country where overseas bonds are held

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Interest Rate Risk

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Interest Rate Risk

Bond prices and yields are inversely related



Interest rate risk often defined as the risk of a fall in bond prices when yields rise



Interest rate sensitivity describes the magnitude of the price move

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Interest Rate Sensitivity



The prices of bonds with longer terms are more sensitive to changes in yield

Bond 1

Term: 6 years
Coupon: 15.0%

The prices of bonds with low coupons are more sensitive to changes in yield

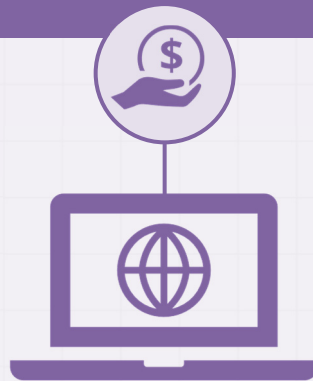
Bond 2

Term: 5 years
Coupon: 1.0%

Investors require ratios to be able to **compare the interest rate sensitivity** between bonds

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Duration

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Measuring Interest Rate Sensitivity



Macaulay Duration



Weighted average maturity of the bond's cash flows

$$D = \frac{\sum_{t=1}^n t \cdot CF_t \cdot (1+YTM)^{-t}}{\sum_{t=1}^n CF_t \cdot (1+YTM)^{-t}} = \frac{\sum_{t=1}^n t \cdot CF_t \cdot (1+YTM)^{-t}}{P_0}$$

The higher the Macaulay Duration of a bond, the higher the bond's sensitivity

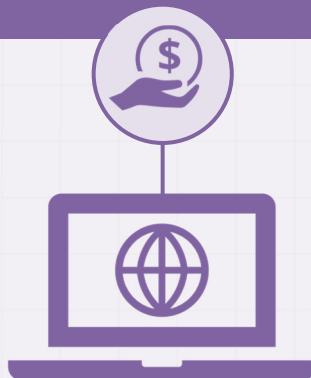
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Macaulay Duration Example

	Year (t)	Cash flow	PV	PV*t	
 <p>5Y bond Annual coupon: 2% YTM: 2%</p>	1	2%	1.96%	1.96%	 <p>Macaulay Duration = 480.77%/100.00% = 4.81</p>
	2	2%	1.92%	3.84%	
	3	2%	1.88%	5.65%	
	4	2%	1.85%	7.39%	
	5	102%	92.38%	461.92%	
		Total:	100.00%	480.77%	

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Modified Duration

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Measuring Interest Rate Sensitivity

Modified Duration



→ Estimate of the relative change in bond price due to a change in YTM

→ Often expressed in %

$$MD = \frac{D}{(1 + YTM/k)}$$

D = Macaulay duration

k = number of payments per year

YTM = yield to maturity

The absolute change in bond price (sometimes referred to as "risk") is given by the product of MD and the dirty price of the bond.

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Modified Duration Example

5Y Bond
Annual coupon: 2%
YTM: 2%



(Macaulay) Duration = 4.81
Current price = 100.00



Modified Duration
= 4.81/1.02
= 4.71



Inverse relationship
between price and yield

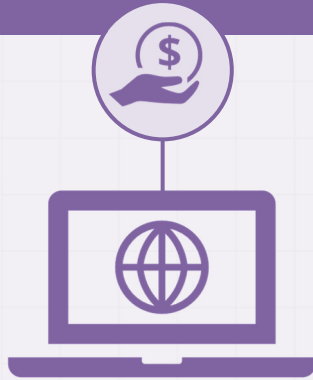
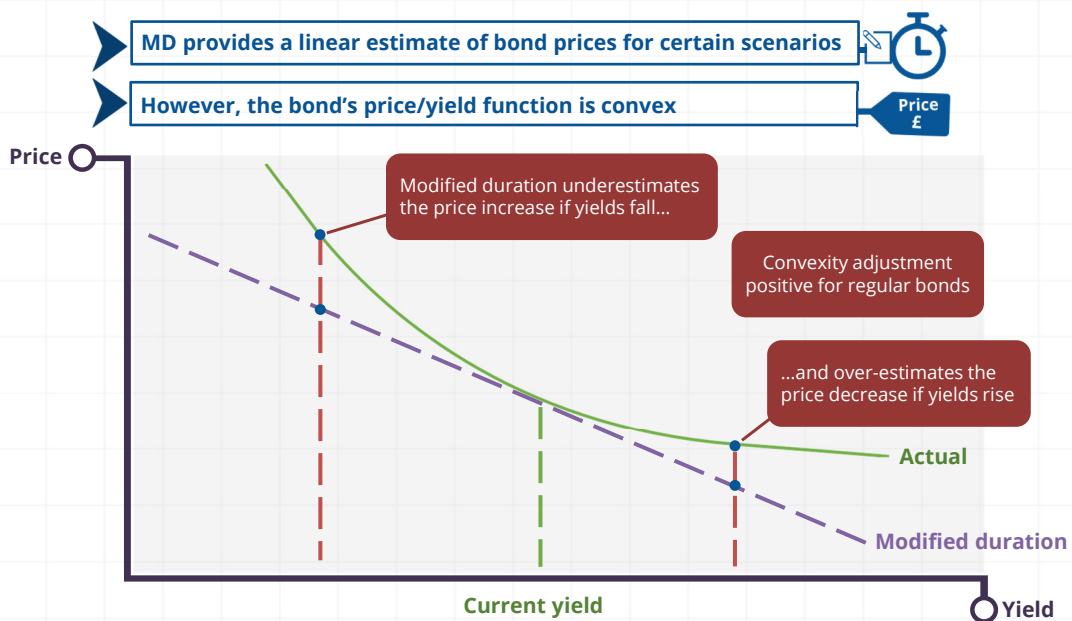
Estimated change in bond price = - Modified duration X Change in yield X Current bond price

If yields rises
by 0.5%

Estimated change in bond price = - 4.71 X 0.005 X 100.00 = - 2.36

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Convexity

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Convexity Adjustment Calculation

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Convexity

$$= \frac{P_+ + P_- - 2P_0}{2 \times P_0 \times \Delta y^2}$$

Convexity adjustment (%)

$$= \text{Convexity} \times 100 \times \Delta y^2$$

Estimated bond price with convexity adjustment

$$= P_0 - \text{MD} \times P_0 \times \Delta y + \text{Convexity} \times P_0 \times \Delta y^2$$

P_0 : Current bond price
 P_+ : New price if rates increase
 P_- : New price if rates decrease

5Y bond, annual coupon:
 2%, YTM: 2%
 MD : 4.71

$$\text{Convexity} = \frac{95.42 + 104.85 - 2 \times 100}{2 \times 100 \times 0.01^2} = 13.68$$

$$\text{Convexity adjustment (\%)} = 13.68 \times 100 \times 0.01^2 = 0.14$$

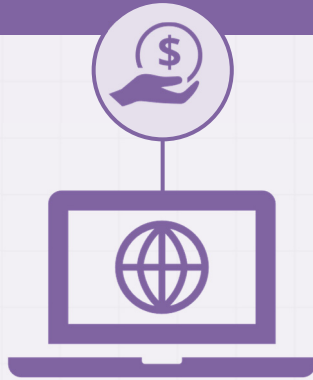
Based on 1% Δy :
 P_0 : 100
 P_+ : 95.42
 P_- : 104.85

If rates fall by 1%:

$$\begin{aligned} \text{New price} &= 100 - 4.71 \times 100 \times 0.01 + 13.68 \times 100 \times 0.01^2 \\ &= 100 + 4.71 + 0.14 \\ &= 104.85 \end{aligned}$$

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DV01

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- Dollar value of 1 basis point

- Shows actual P&L impact in \$ terms for a 1 basis point change in yields

$$DV01 = \frac{P_d * MD(\%) * FV}{100}$$

For single bonds DV01 can be calculated based on MD

DV01 considers both: the sensitivity of a bond and the position size

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DV01 Example



5Y bond
Annual coupon: 2%
YTM: 0.35%



MD = 4.80
 $P_d = 108.16\%$
Position size: 100 million



$$DV01 = 108.16\% * 4.80\% * \$100,000,000/100 = \$51,914.25$$

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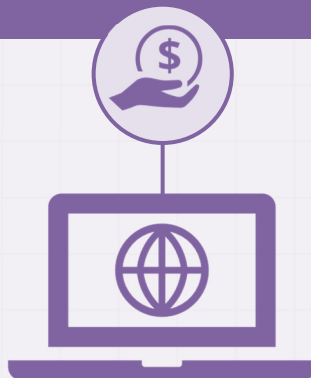
Approaches to Liability Matching

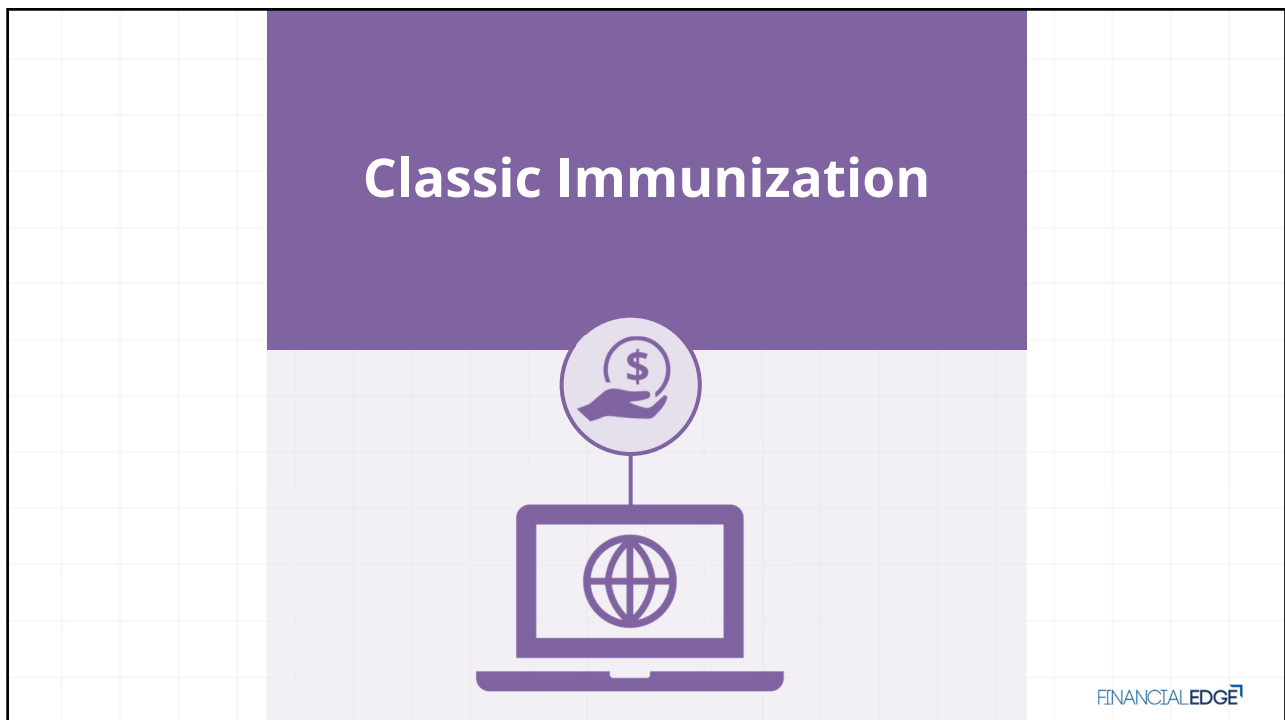
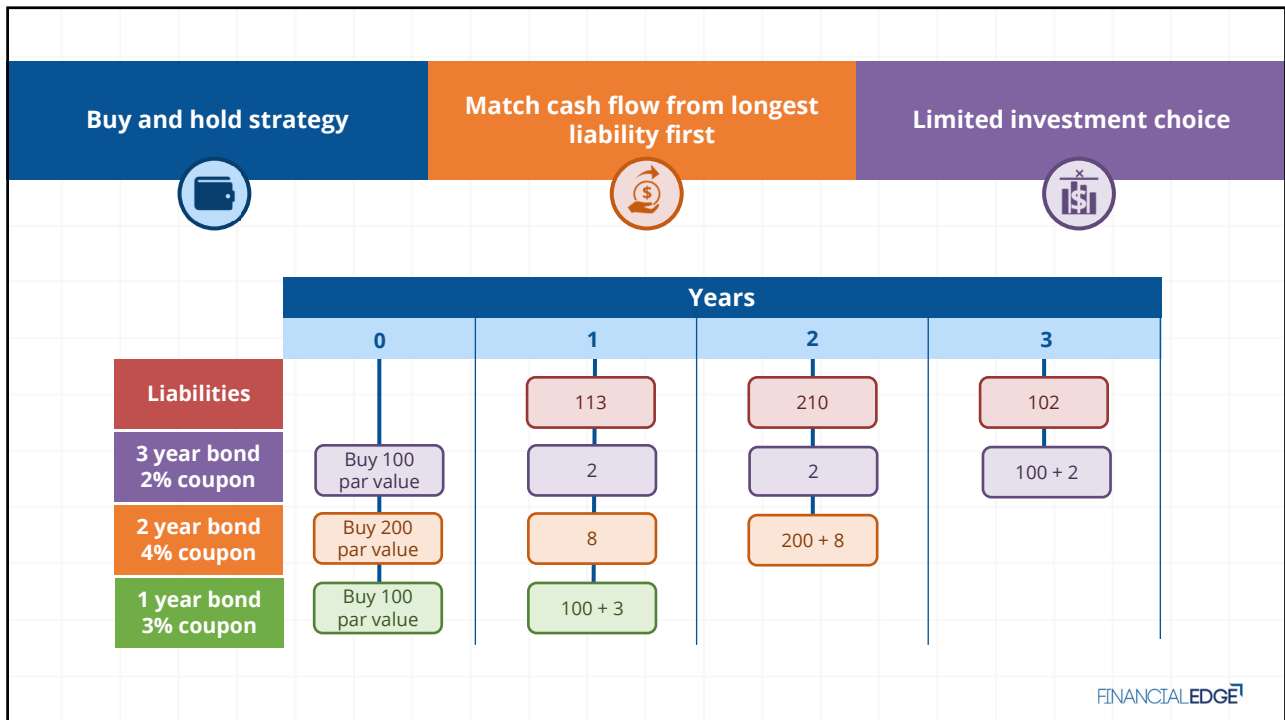
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	Cash Flow Matching	Duration Matching (Immunization)
Description	Construct a portfolio of bonds whose future cash flows will meet future liabilities	Construct a portfolio of bonds whose duration matches the duration of the liability
Advantages	Simple buy and hold strategy removes exposure to interest rate risk	Wide variety of bonds can be used
Disadvantages	Bonds may not be available to match timings of liabilities precisely	Requires monitoring and rebalancing

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Cash Flow Matching

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The interest rate risk of a portfolio used to meet a single future liability can be almost eliminated by holding a bond, or portfolio of bonds for which the duration of the bond(s) matches the duration of the liability

				Value at time 4.5, if rates are:		
Liability (years)	4.5	Year	Cash flows	3.0%	4.0%	5.0%
Bond:		1.0	5.86	6.49	6.72	6.95
Maturity	5.0	2.0	5.86	6.31	6.46	6.62
Coupon rate	5.86%	3.0	5.86	6.12	6.21	6.30
Par value	100.0	4.0	5.86	5.94	5.98	6.00
Duration (years)	4.5	5.0	105.86	104.30	103.80	103.31
				129.17	129.17	129.17

Coupons reinvested until time 4.5 earning interest

Sale proceeds at time 4.5 are the present value of remaining cash flows

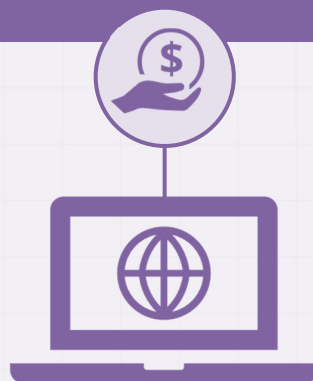
Duration of bond matches time until liability is due

If rates fall, lower interest on coupons but higher sale proceeds

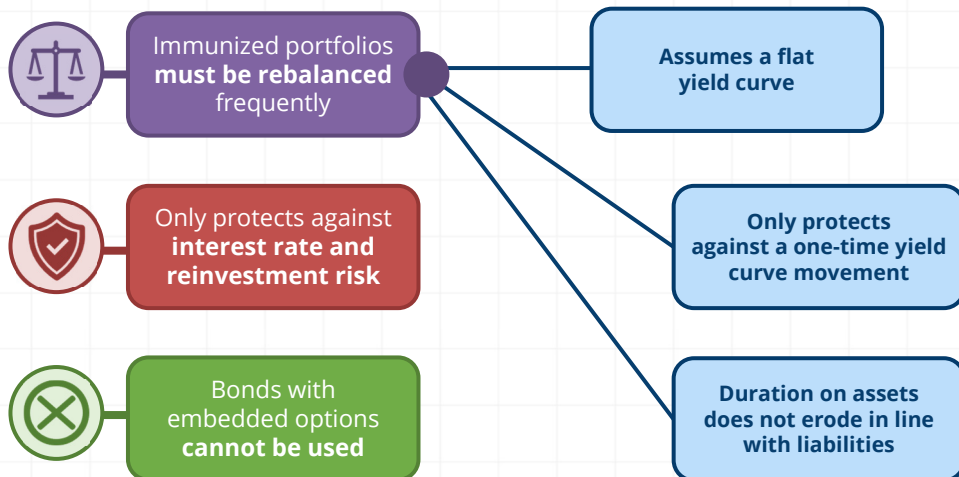
If rates fall, lower interest on coupons but higher sale proceeds

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Problems with Immunization

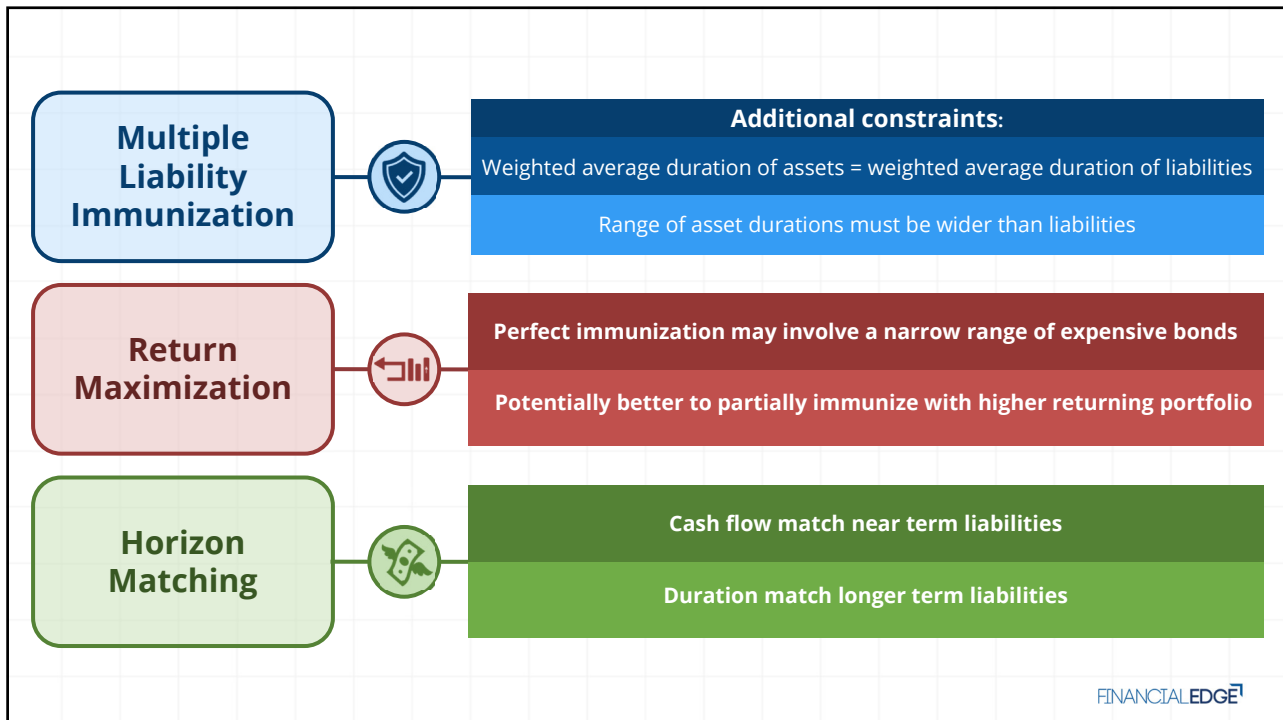
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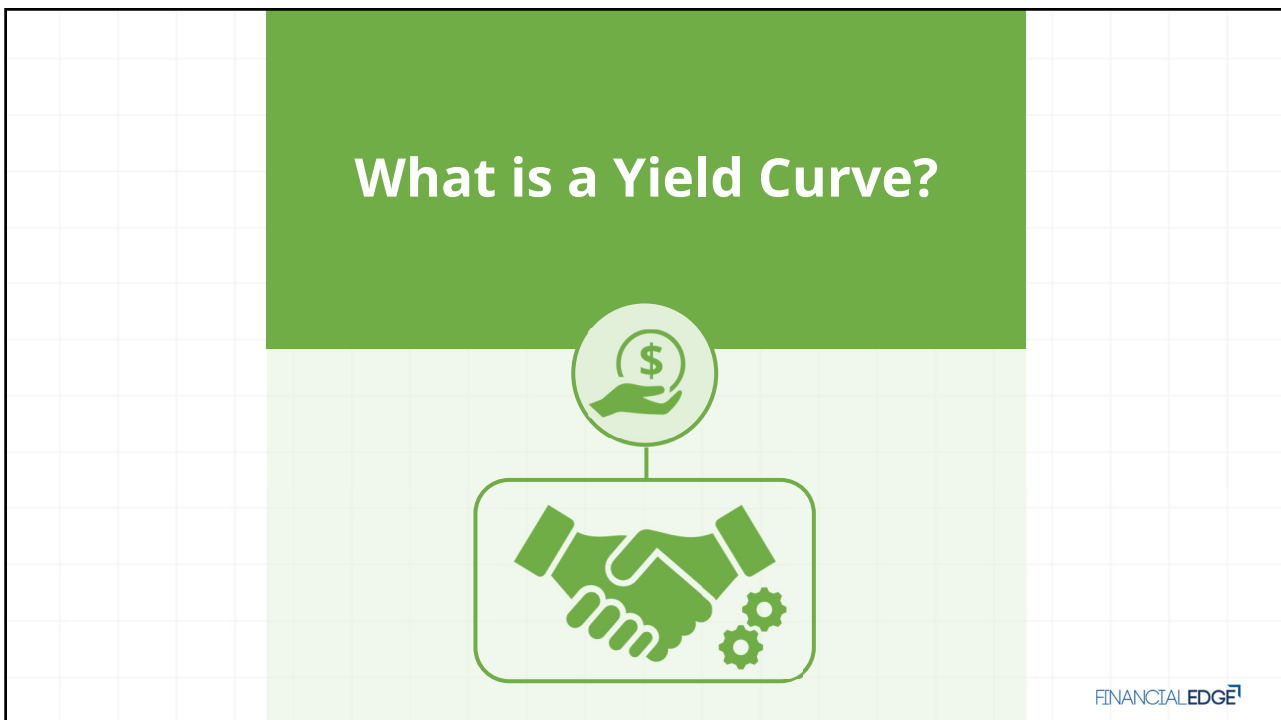
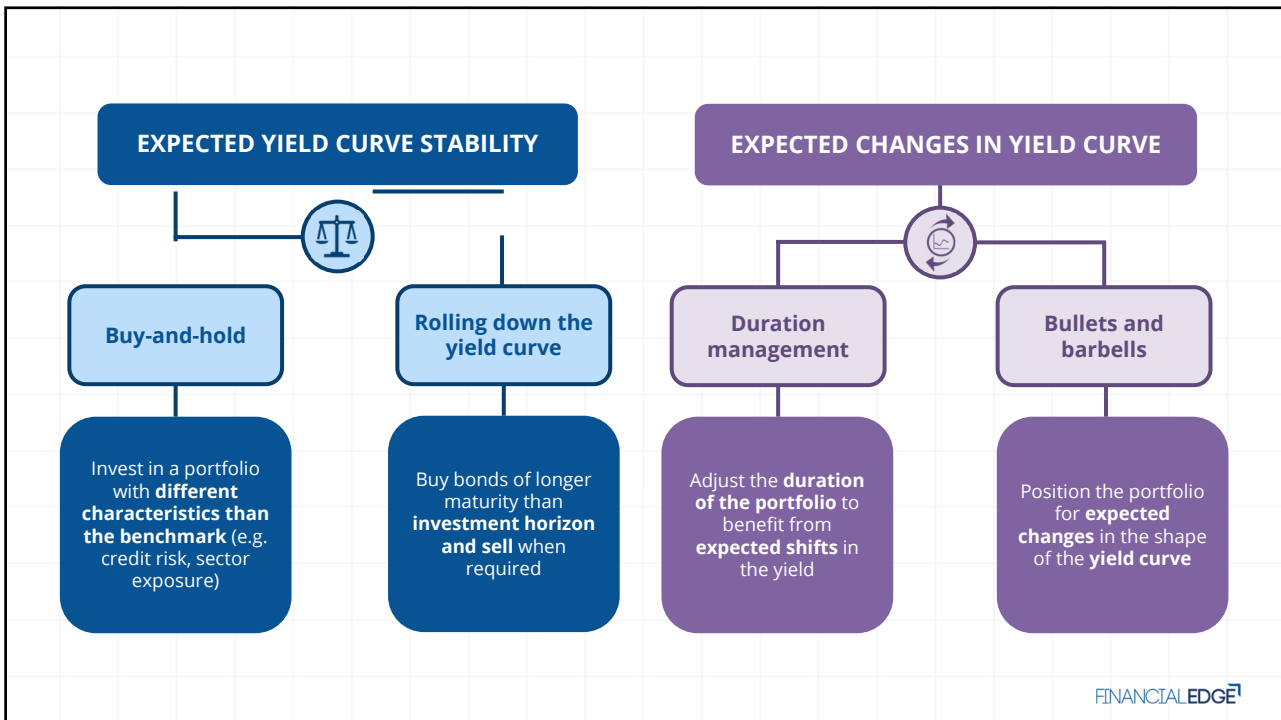
Problems With Classic Immunization

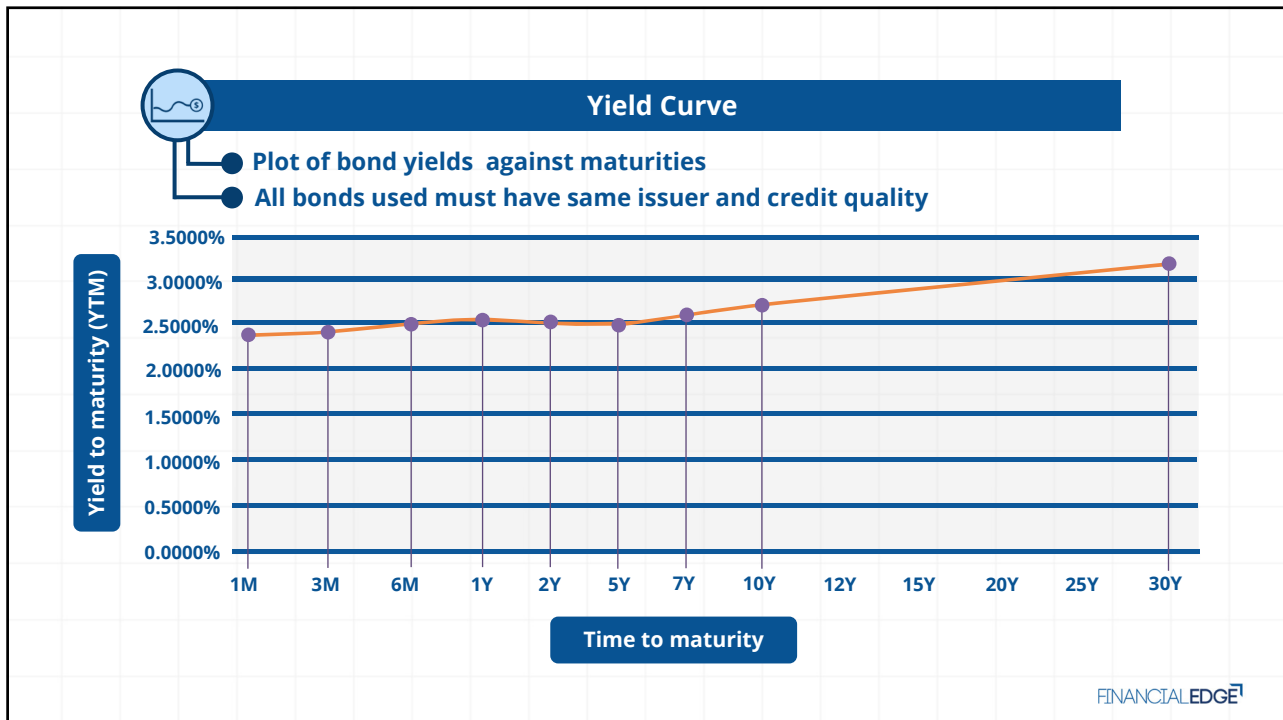
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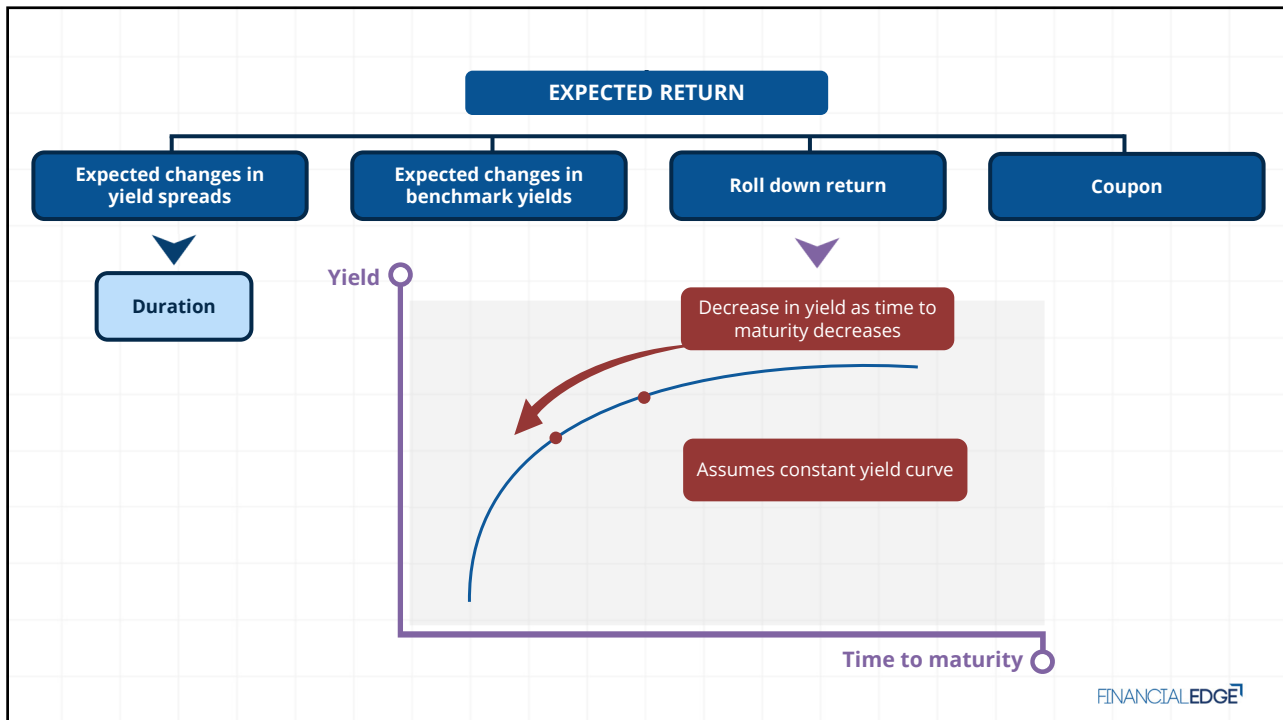
Extensions to Immunization

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Rolling Down the Yield Curve





Buy Longer Dated Bond That Investment Horizon and Sell Bond as Needed

Example 3-month investment horizon

	Buy and hold 3-month Treasury Bill	Buy 6-month Treasury Bill and sell after 3 months
Purchase price	99.50 (3m T-Bill)	98.80 (6m T-Bill)
Cash flow in 3 months	100 (Par value)	99.50 (now a 3m T-Bill)
3 month holding period return	$= (100 - 99.50) / 99.50$ $= 0.50\%$	$= (99.50 - 98.80) / 98.80$ $= 0.71\%$

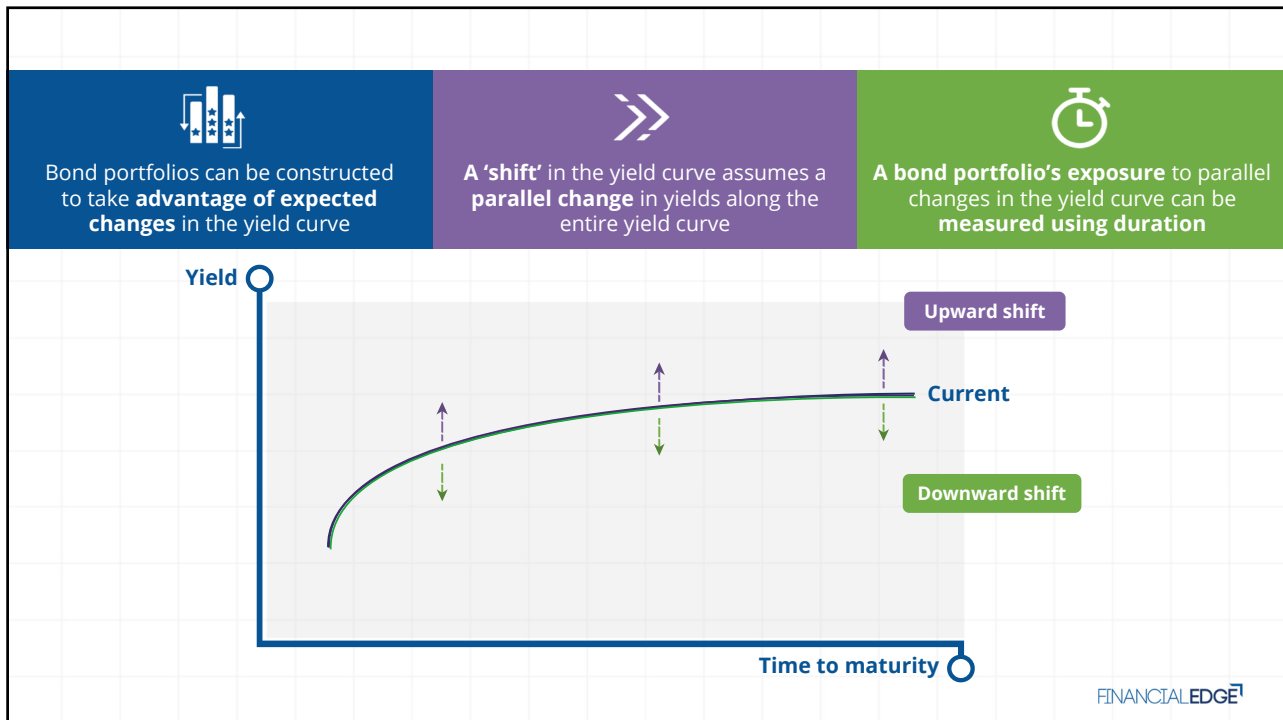
0.21% more return than buy and hold

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Active Bond Portfolio Management – Yield Curve Shifts



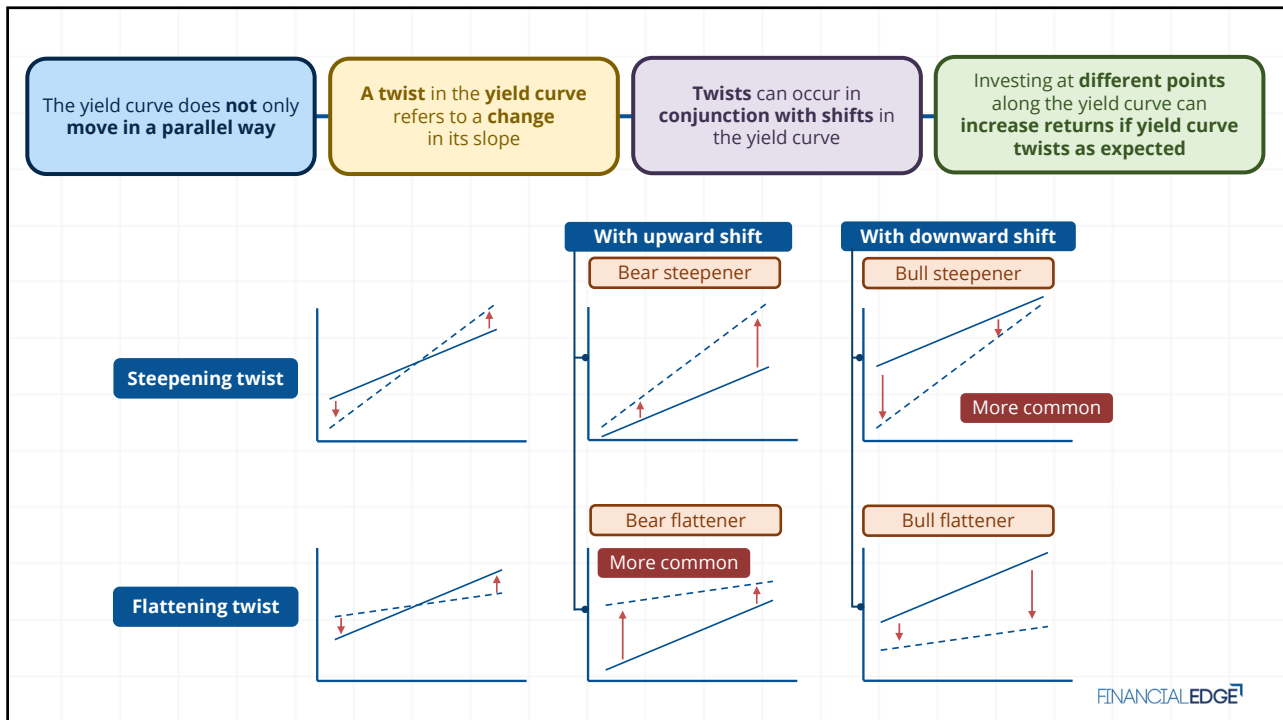
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Expectations of an upward shift in the yield curve	Expectations of a downward shift in the yield curve
Higher interest rates mean lower bond prices	Lower interest rates mean higher bond prices
Reduce portfolio duration to increase exposure to falling bond prices	Increase portfolio duration to increase exposure to increasing bond prices
Sell longer dates bonds, buy shorter dated bonds	Sell shorter dates bonds, buy longer dated bonds
Sell bond futures	Buy bond futures
Pay fixed on interest rate swaps	Receive fixed on interest rate swaps

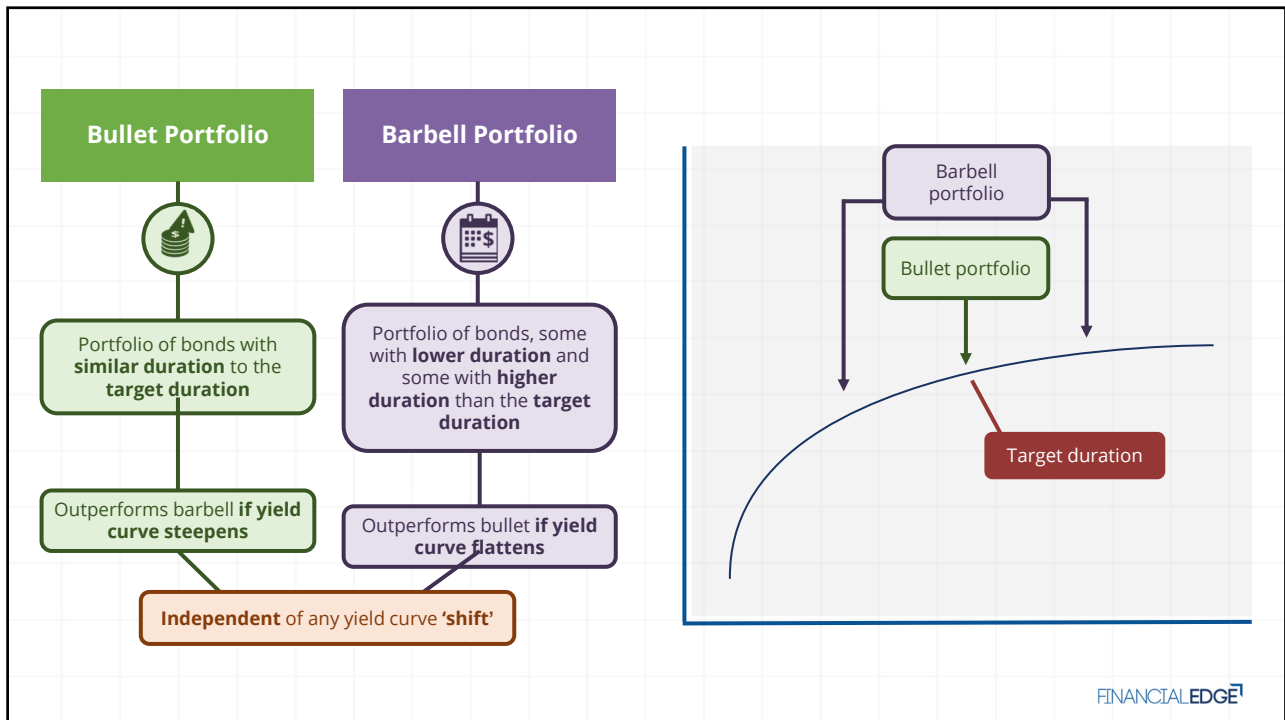
Active Bond Portfolio Management – Yield Curve Twists





Active Bond Portfolio Management – Bullets & Barbells





Using Derivatives to Manage Interest Rate Risk



Using Derivatives to Manage Interest Rate Risk

Bond futures can be used to **manage interest rate risk**

A long bond futures position will **pay a gain** if interest rates fall

A short bond futures position will **pay a gain** if interest rates rise

The number of futures contracts to trade?



$$\frac{(\text{Target duration} - \text{Portfolio duration})}{\text{Duration of futures contract}} \times \frac{\text{Portfolio market value}}{\text{Futures contract value}}$$

Futures contract value



$$\text{Futures price (per \$1 of nominal value)} \times \$100,000$$

The contract size for **each future** is \$100,000

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