



Bonds and the Yield to Maturity

Bonds Overview



Main Principles of Bonds



Debt instruments



**Typically fixed
maturity date**



**Typically regular
interest payments**

Coupon

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What distinguishes a bond from a loan?



BONDS

Offer greater liquidity

A relatively active secondary market

Bonds can be sold before maturity



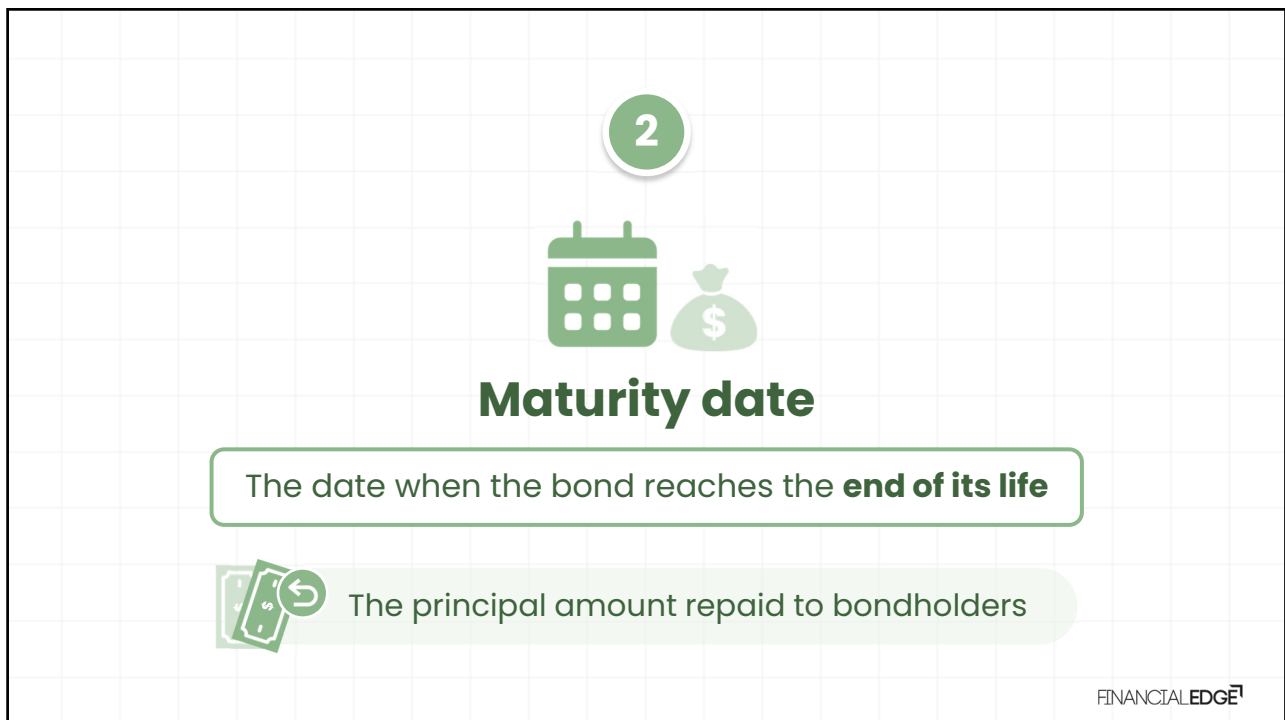
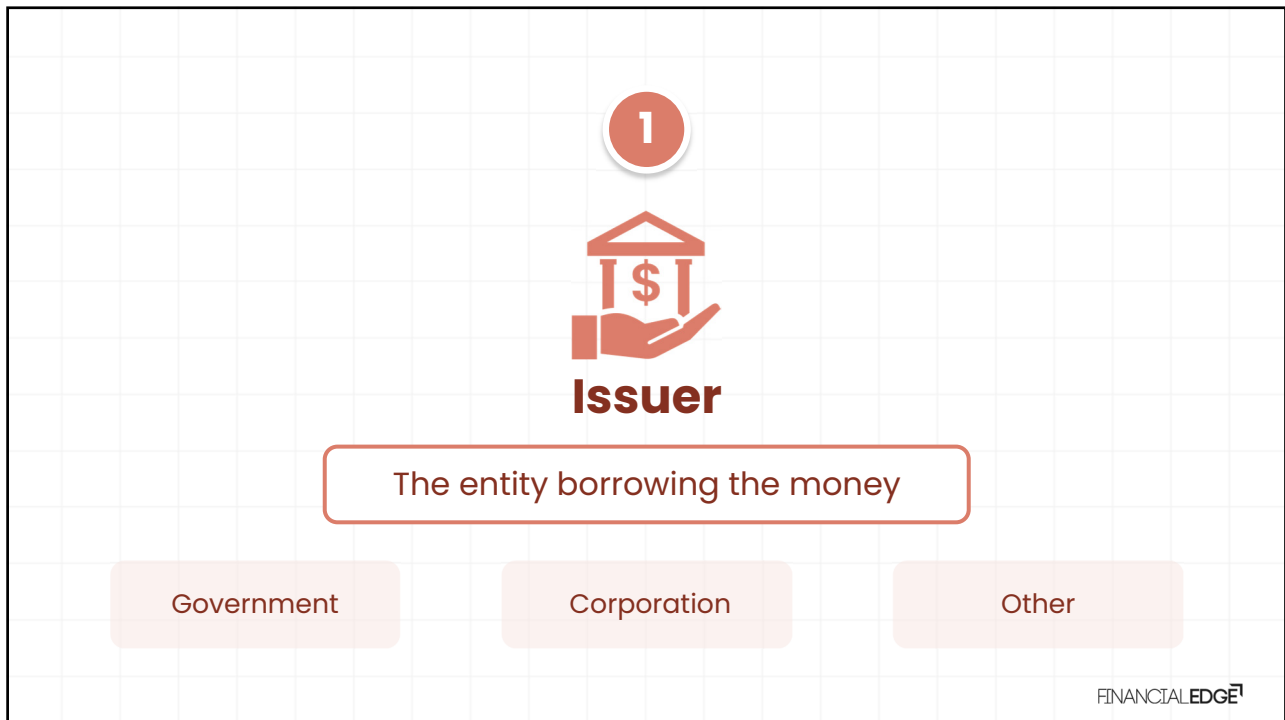
LOANS

More complex to sell

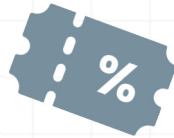
Require more time to completion

Higher transaction costs

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3



Coupon

The **interest rate paid** to the bondholder on a regular basis



The income an investor earns for holding the bond

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Par value/face value

(Principal amount or notional)

The amount of money the bondholder will be repaid at the bond's maturity

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**Price**

The bond's current market value (percentage of face value)



Bond prices fluctuate due to **interest rate movements**

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Bond Price Quotation

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Bond markets have evolved over time
in terms of **how they quote prices**



Fractional Quotation

Decimal Quotation

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Fractional Quotation

Decimal Quotation



U.S. Treasury Bonds

Historically, U.S. Treasury Bonds were quoted in fractions, specifically in 32nds of a dollar

U.S. Treasury note with a
quoted price of 100-7

The bond is trading at **100** and
7/32nds of its par value

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Fractional Quotation**Decimal Quotation**

Example bond:	US Treasury Note
Quoted price:	100-7
Interpretation:	The bond is trading at 100 and 7/32nds of its par value
Decimal equivalent:	100.2188%
Par value:	100,000 USD
Price in USD	100,218.80 USD

FINANCIALEDGE⁷**Fractional Quotation****Decimal Quotation**

A gradual shift towards decimal pricing started in the early 2000s

Modernize and **simplify**
bond trading

Align bond markets with broader trend in
financial markets towards **decimalization**

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Fractional Quotation

Decimal Quotation



European and Other International Markets

Widely used metric system

Global trend towards **decimalization** in financial markets

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Fractional Quotation

Decimal Quotation



Example bond:	Japanese government bond
Quoted price:	100.9290
Interpretation:	The bond is trading at 100.9290% of its par value
Par value:	100,000,000 JPY
Price in JPY:	100,929,000 JPY

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Fractional Quotation

Decimal Quotation



Emerging Markets

The quoting convention can vary

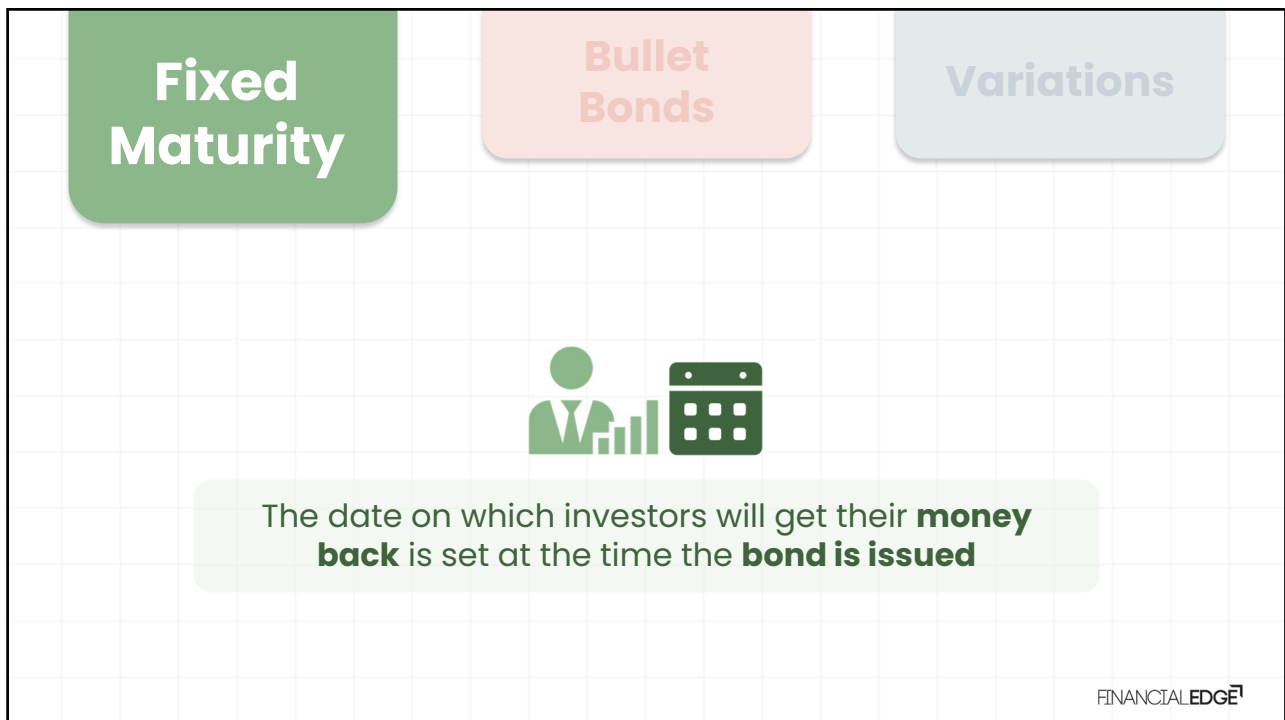
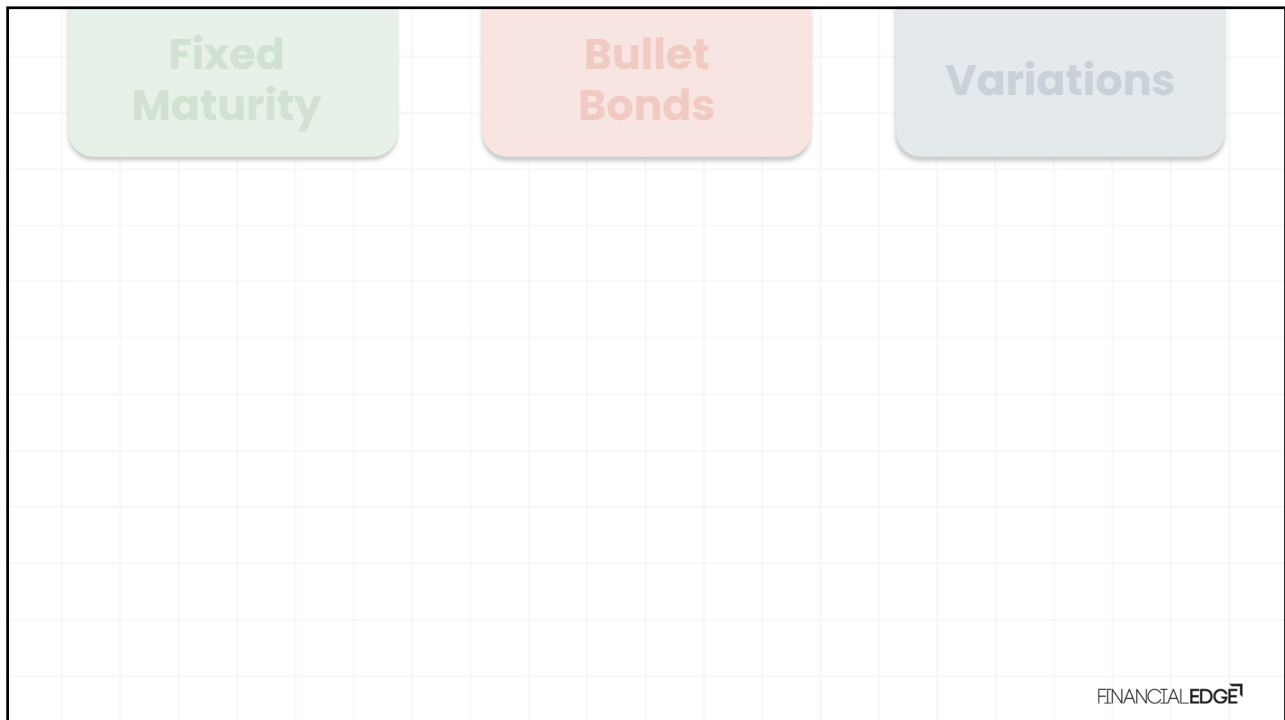
Transitioning to
decimal pricing

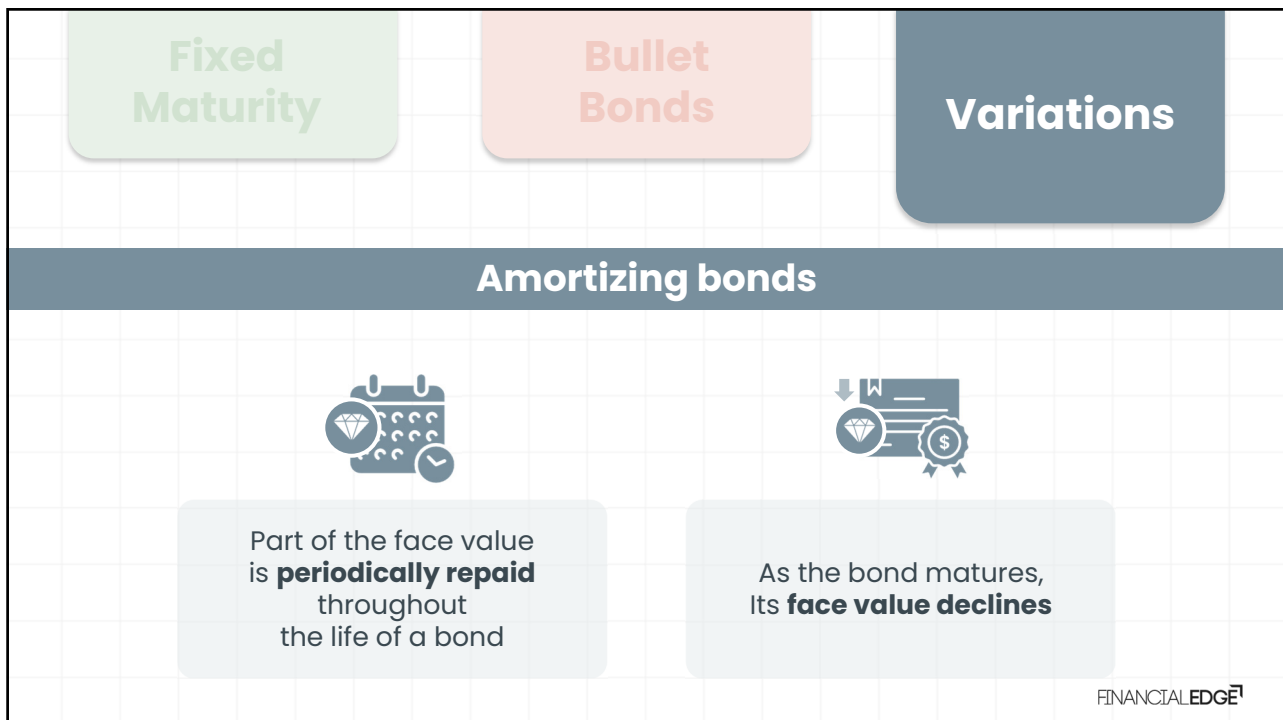
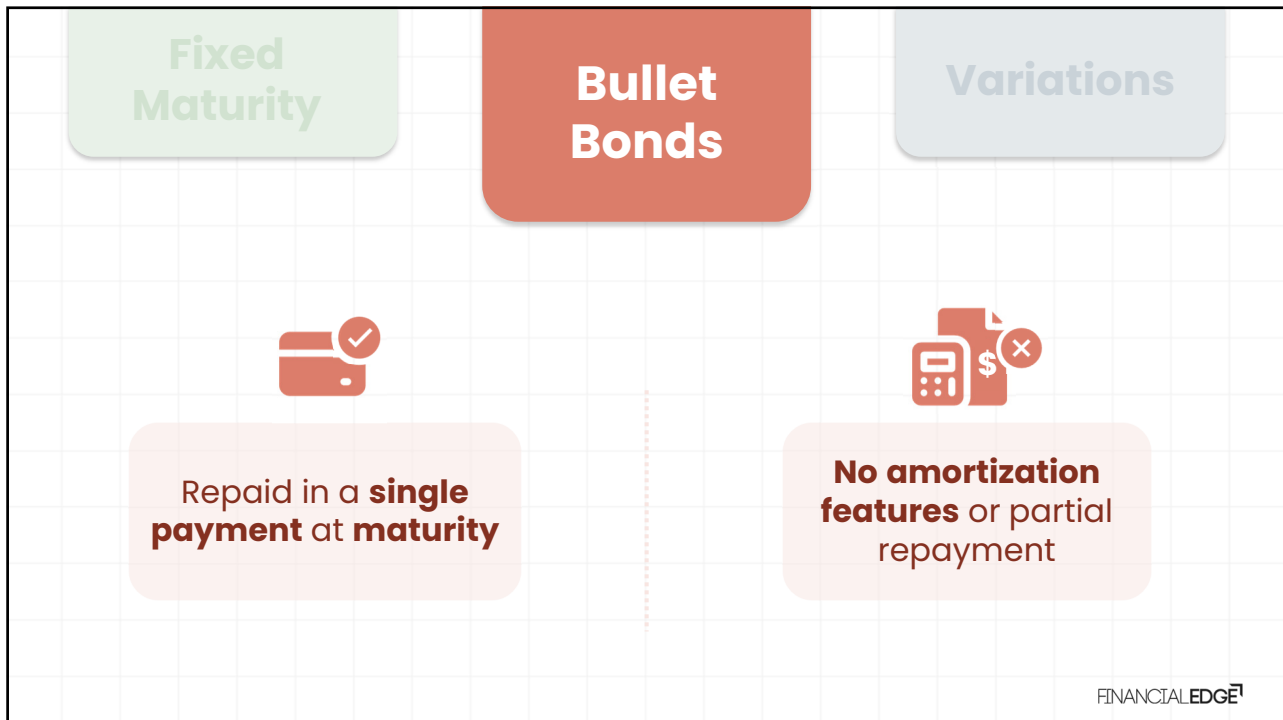
Aligns with **international
standards**

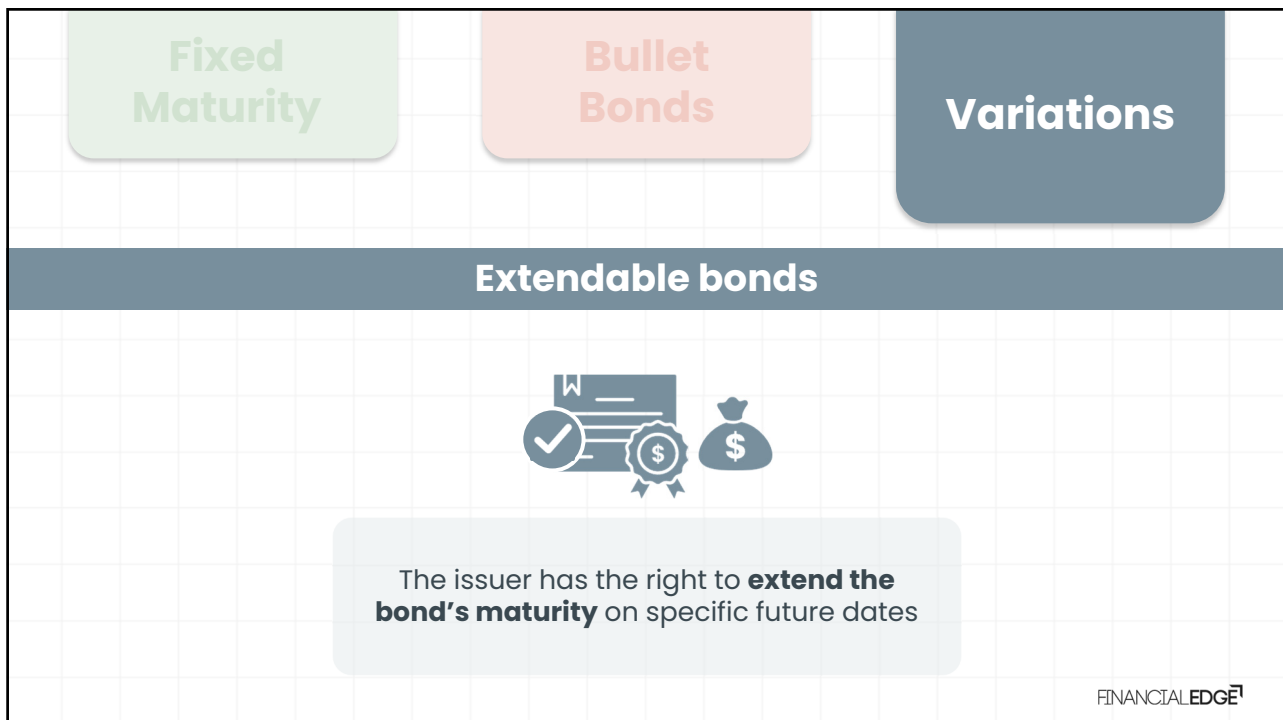
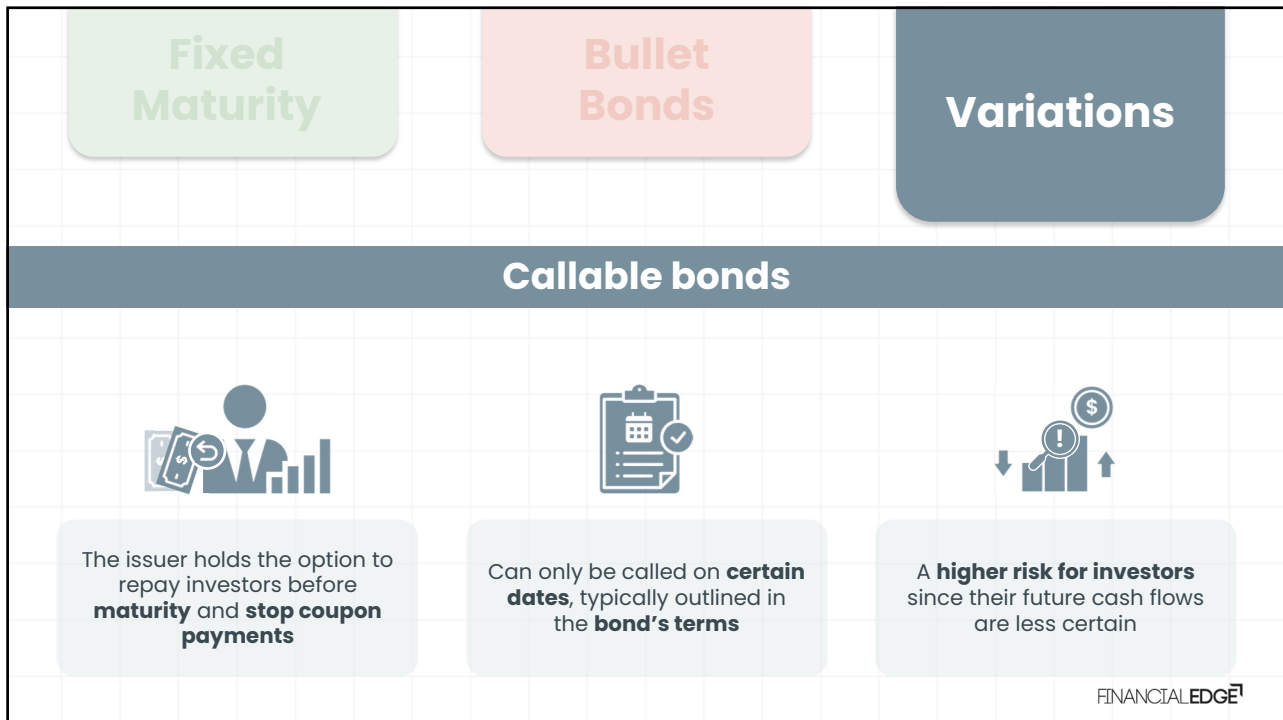
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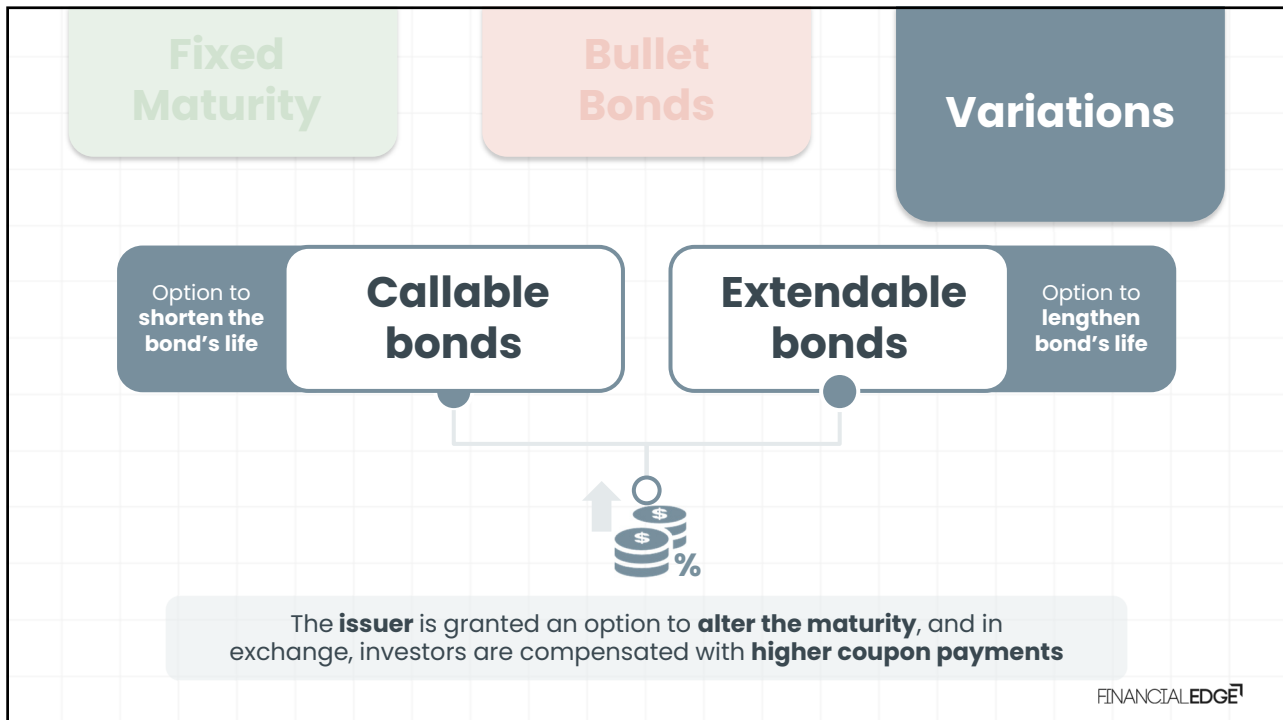
Bond Redemption

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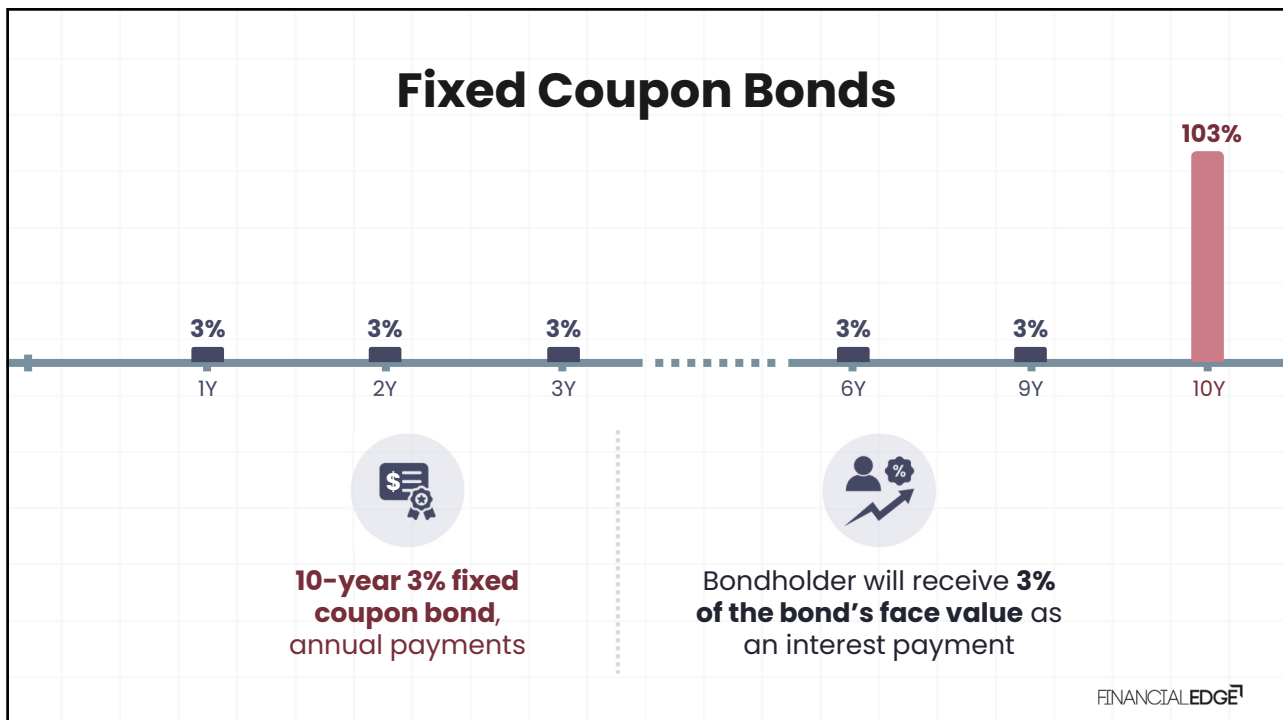
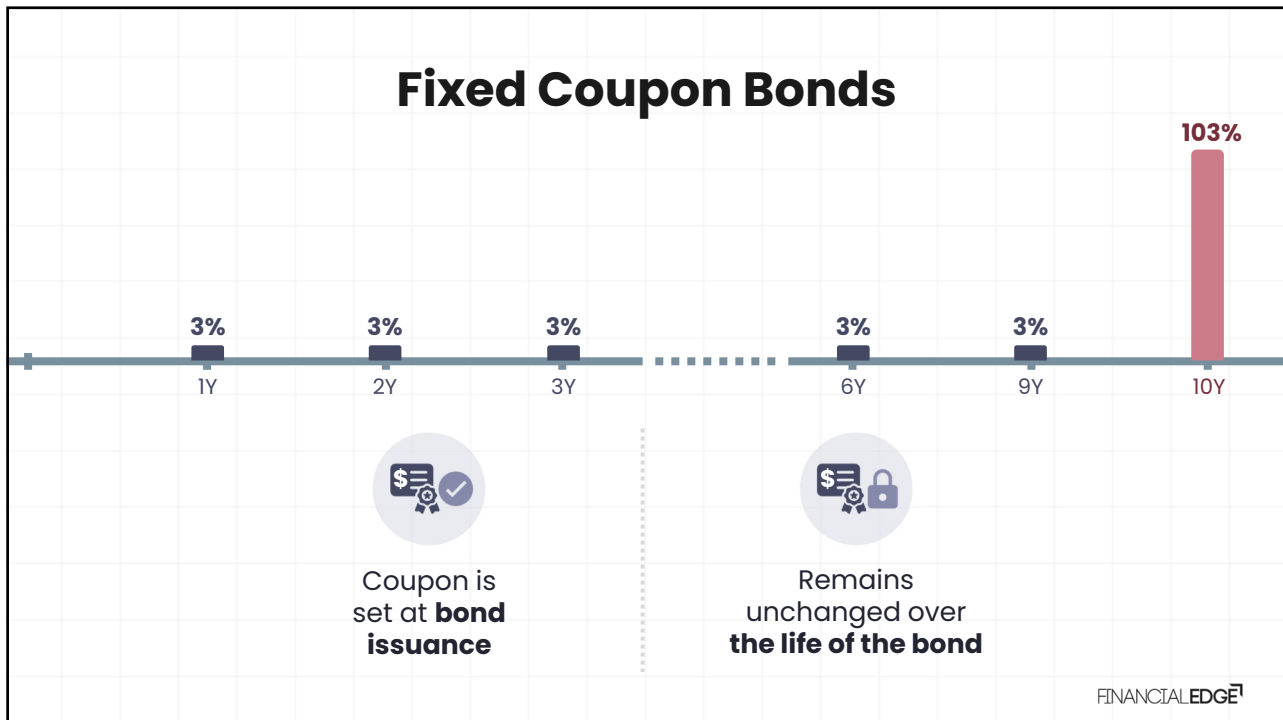




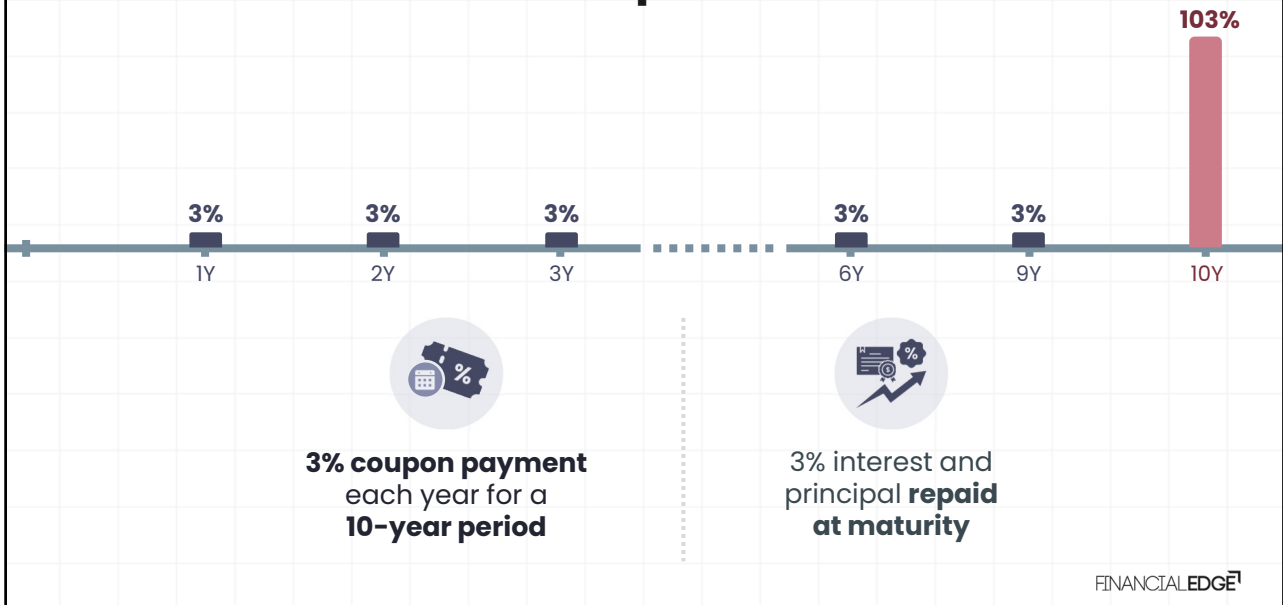




Fixed Coupon Bonds

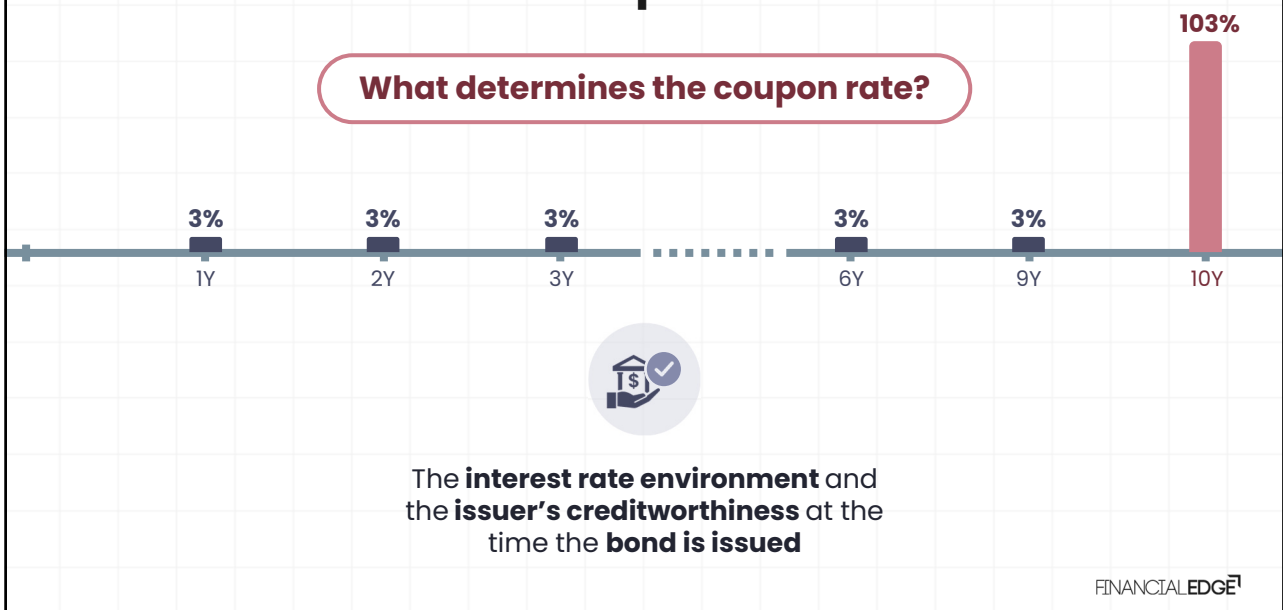


Fixed Coupon Bonds



Fixed Coupon Bonds

What determines the coupon rate?



Zero Coupon Bonds

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Zero Coupon Bonds

10-year zero bond, issued at 74.51%, repaid at 100%

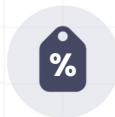
100%

10Y

-74.51%



No interest payment
between **issuance** and
maturity of the bond



Sold at a **discounted**
price, repaid at 100%



The return is given by the
difference between **issue**
and **redemption price**

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Floating Rate Notes (FRNs)

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Floating Rate Notes (FRNs) or “floaters”
are bonds with variable rates



Coupon formula is
set when the **bond**
is issued



References IBOR
(Interbank Offered Rate)
or the newer **risk-free**
rates (RFRs)

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Floating Rate Notes (FRNs) Examples

**IBOR (EURIBOR)****RFR (SOFR)**

Interbank Offered Rates (IBOR)
Euro Interbank Offered Rate (EURIBOR)

Risk-Free Rate (RFR)
Secured Overnight Financing Rate (SOFR)

FINANCIALEDGE⁷**IBOR (EURIBOR)****10-year FRN**

PAYS

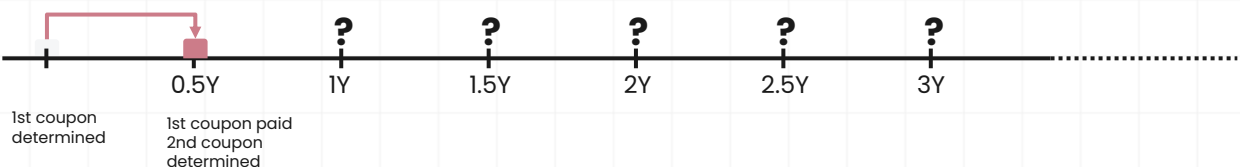
6M EURIBOR

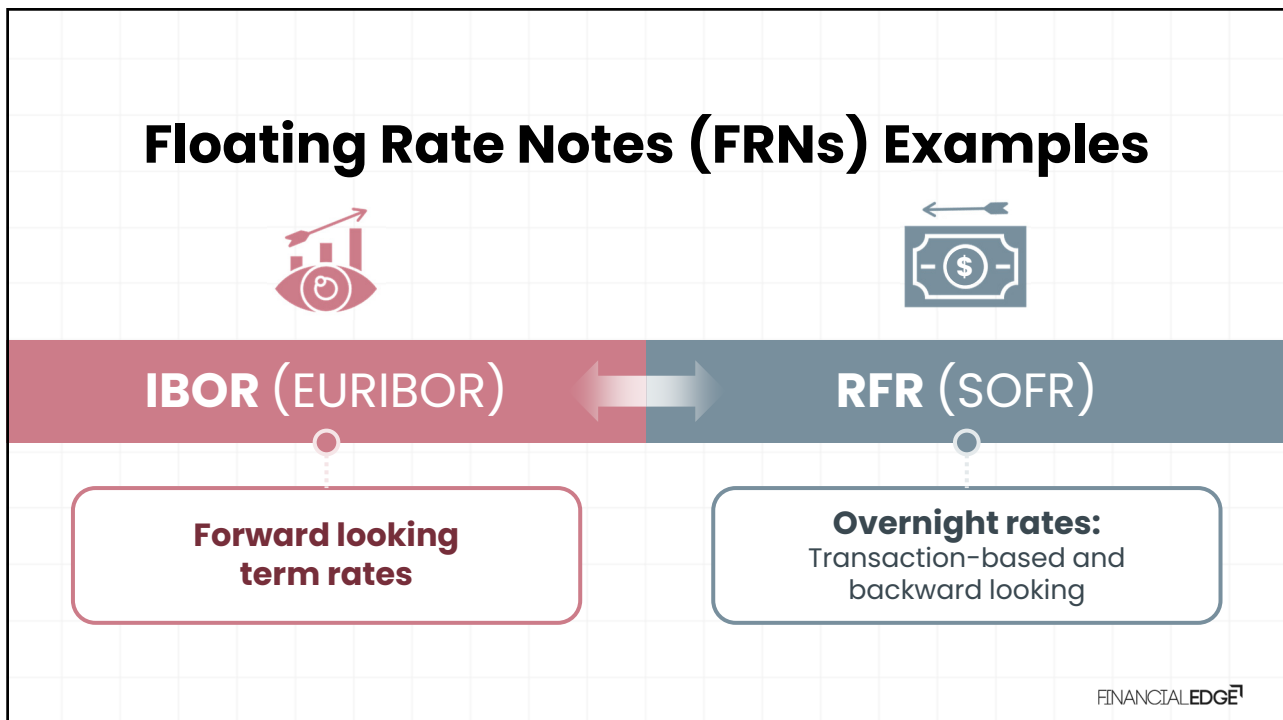
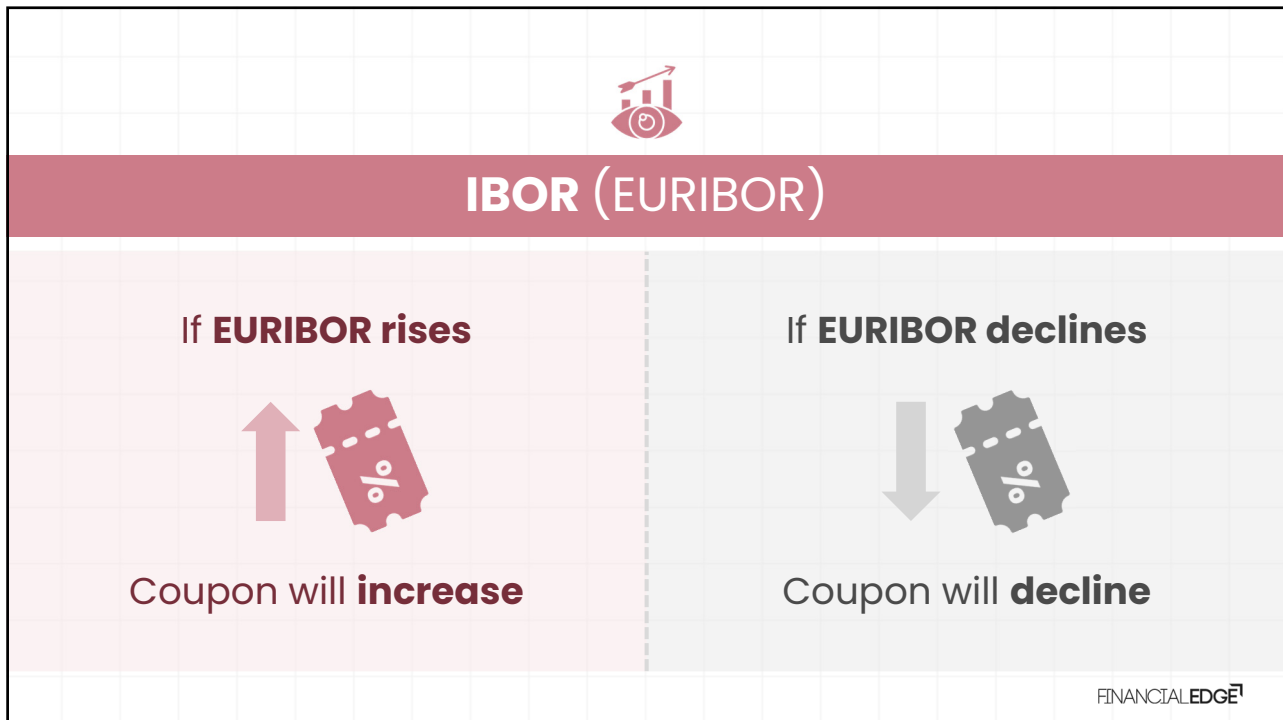
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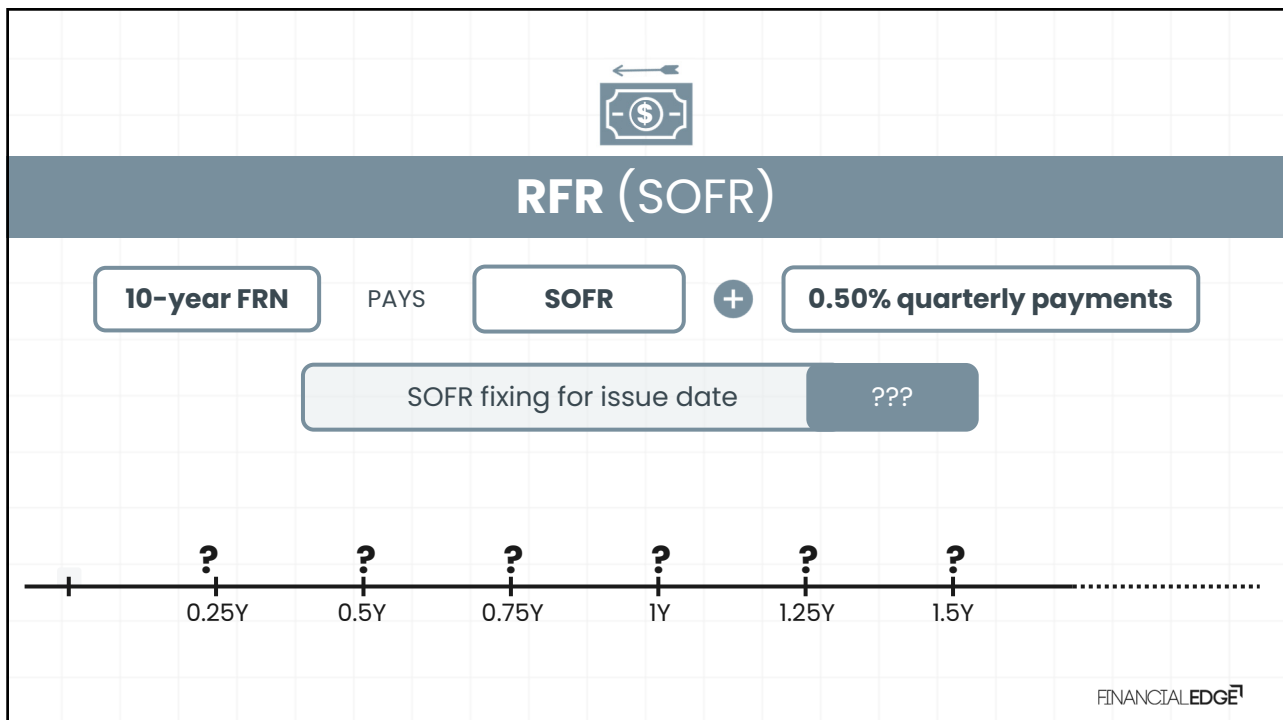
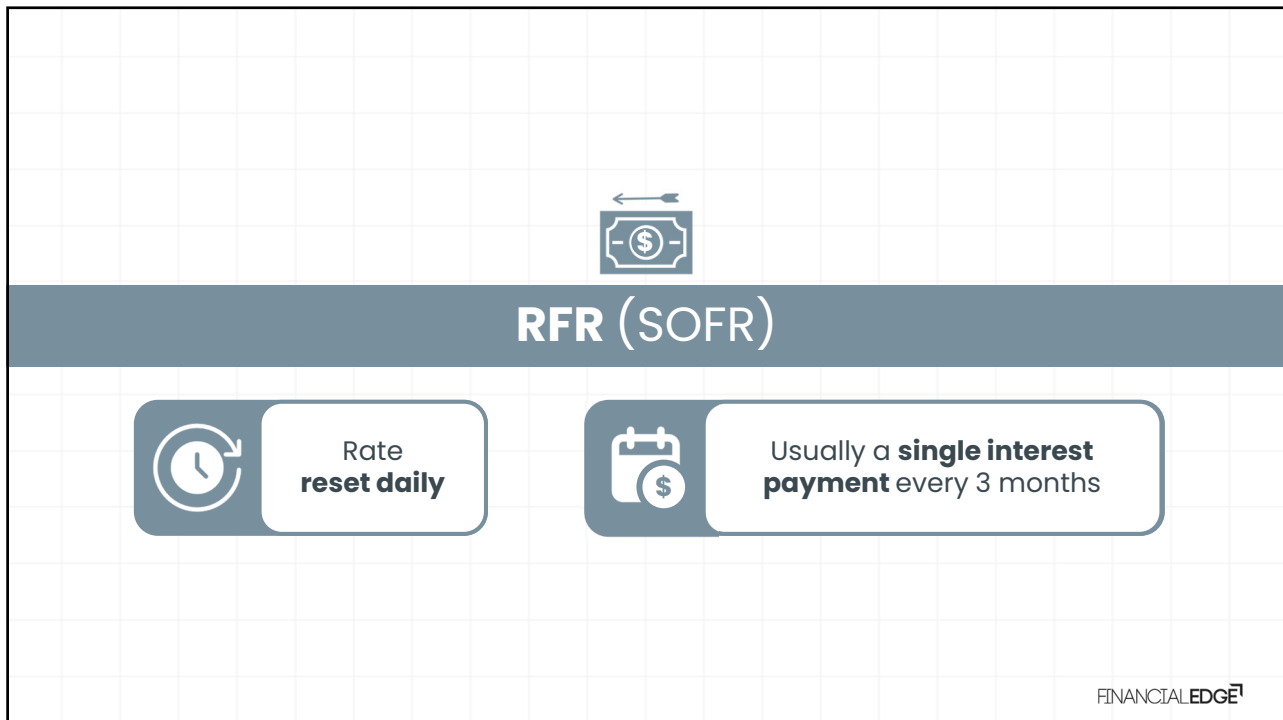
0.50% payments**semi-annual**

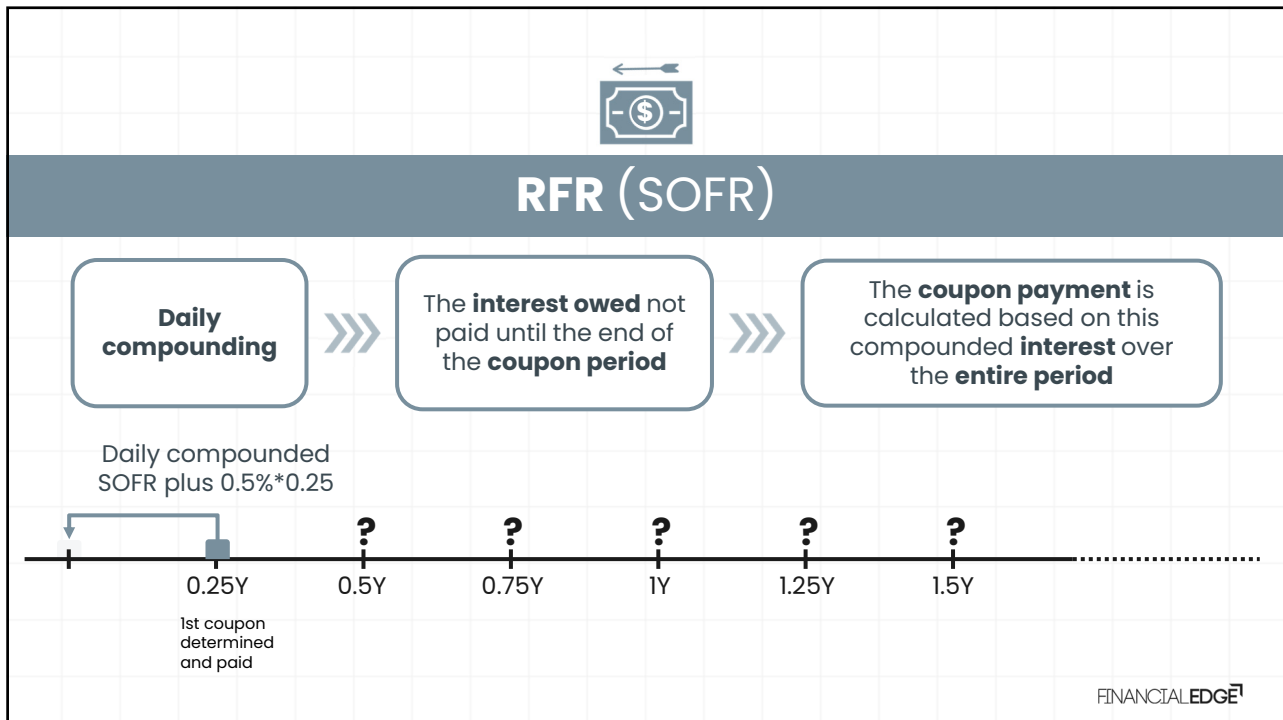
6M EURIBOR fixing for issue date

3.96%

 $4.46\% \times 0.5$ FINANCIALEDGE⁷







Pricing a Fixed Coupon Bond – The General Approach



Bonds are **often quoted in price terms**

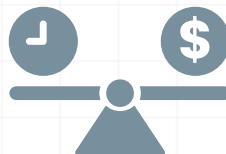


Price

Showing the **percent of notional** that an investor must currently pay for the bond



How can a bond be priced?

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Time Value of Money (TVM)



The **present value** of a **cash flow** is **different** from its **future value**



Present money has the potential to earn **interest or investment returns**, while future money is **not immediately** available for use

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In case of fixed coupon bonds cash flows are known in size and timing

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$\text{Coupon Bond Price} = \frac{C_1}{(1+r)^1} + \frac{C_2}{(1+r)^2} + \frac{C_n + FV_n}{(1+r)^n}$	
C	Coupon amount per period
FV	Face value
r	Required rate of return, per period
n	Number of periods to maturity

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The price of a bond is the **sum of the present values** of all **outstanding coupon payments** and the **redemption payment**

$$\text{Coupon Bond Price} = \frac{C_1}{(1+r)^1} + \frac{C_2}{(1+r)^2} + \frac{C_n + FV_n}{(1+r)^n}$$

C	Coupon amount per period
FV	Face value
r	Required rate of return, per period
n	Number of periods to maturity



At **issuance**, the **bond price** is set so that:



Coupon payments



Final redemption value



Investors achieve their required rate of return



Bond price in the secondary market



Supply and
demand factors



Changes in
interest rates



Changes in
issuer's
creditworthiness



Premium (above face value)



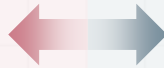
Discount (below face value)

Government Bond Issuance - Overview

Bond Pricing – Practical Example



Government Bond



Corporate Bond



The process leading to the **actual pricing** might differ



Government Bond



Issued via
public auctions



The issuer **places securities** directly
with **investors**



Investors submit
orders for the
yield they desire

Bond Pricing – Concrete Example

\$10 billion of a 5-year bond via auction

Yield	Demand	Aggregated demand
4.522%	3.4 bn USD	3.4 bn USD
4.523%	4.9	8.3
4.524%	2.5	10.8
4.525%	1.3	12.1
4.526%	1.1	13.2
4.527%	0.5	13.7

**Highest
accepted
yield**

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Yield to Maturity

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In the **secondary market**, the bond price is typically determined by:

Supply



Demand

✗ Pricing calculations are **less necessary** ✗



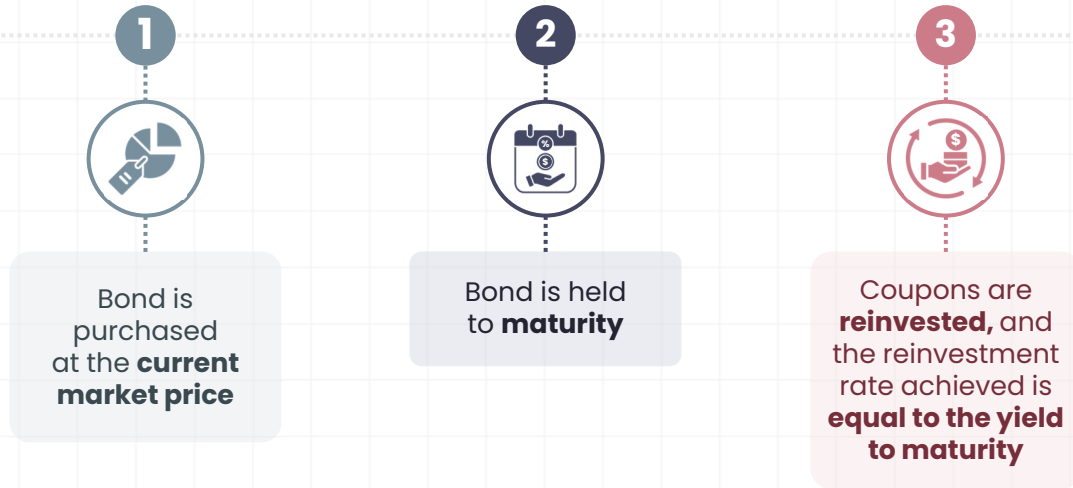
Investors are keen to understand **the return** they would provide

Yield to Maturity (YTM)

Solve for **r** so that: $\frac{C_1}{(1+r)^1} + \frac{C_2}{(1+r)^2} + \frac{C_n + FV_n}{(1+r)^n} = \text{market price of bond}$

Adjusting the **discount rate** used in the formula shown until the sum of the **bond's future cash flows equals** its current **market price**

YTM based on the following assumptions:



Constant **reinvestment rate** for all coupons **equal to the YTM** at the time of the bond purchase

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Yield to Maturity Components

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Yield to Maturity (YTM)

Coupons

Reinvestment
returns

Bond price

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Coupons

Interest payments



Bond issuer



Bondholder

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Yield to Maturity (YTM)

Coupons

Reinvestment
returns

Bond price

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Reinvestment returns



Potential returns earned if the **bondholder reinvests** the **coupon payments** at the **same rate** as the **bond's YTM until maturity**



Coupon payments



Bond's notional
(principal) amount

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Yield to Maturity (YTM)

Coupons

Reinvestment
returns

Bond price

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Bond price

 **INVESTOR**

Buys a bond at a **price below par** and the **bond is redeemed at par**



CAPITAL GAINS



Purchases a bond at a **price above par** and the **bond is redeemed at par**



CAPITAL LOSSES

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The Bond Price/Yield Relationship

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**Bond
Price**

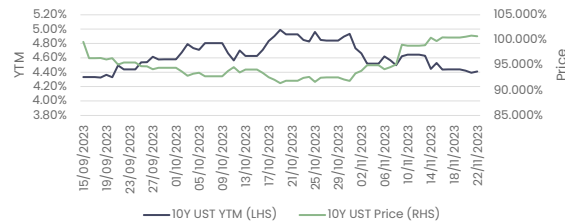
CLOSE LINK



**Bond
Yield**

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Bond Price/Bond Yield Relationship



Bond yield reflects...



Coupon payments



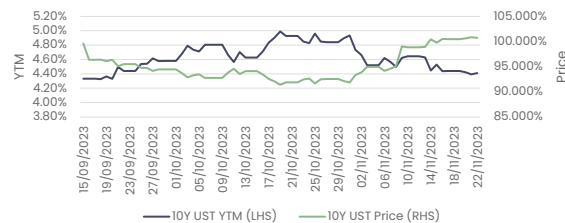
Capital gains or losses



Redemption payment

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Bond Price/Bond Yield Relationship



Price of a bond rises



Yield of the bond falls

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10-year bond with a 4% fixed coupon at a price of 92% of its face value

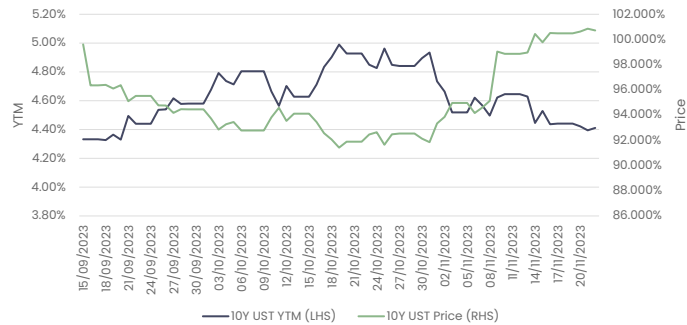


4% coupon annually



Buying the bond at 92%

100% at maturity



Price of a bond rises



Yield of the bond falls

VICE VERSA

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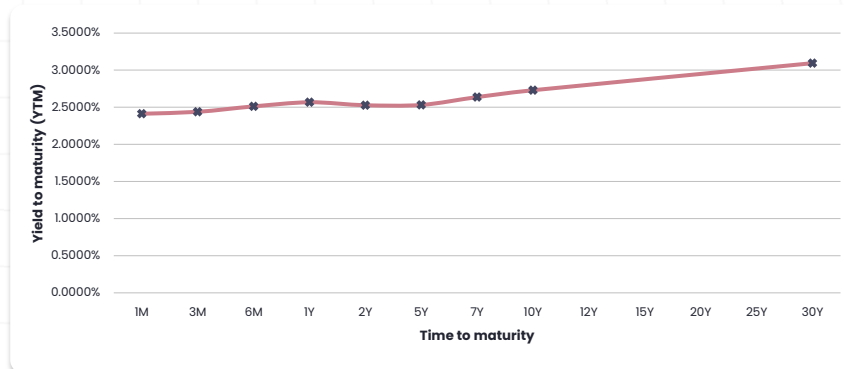
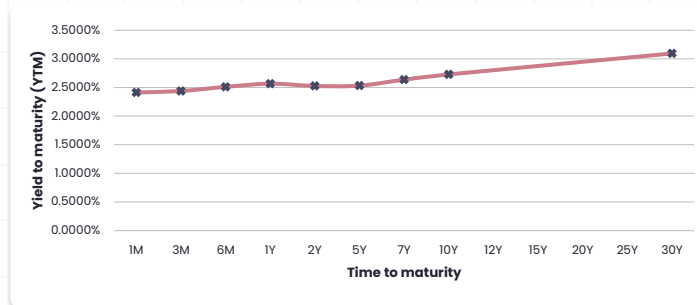
Yield Curve

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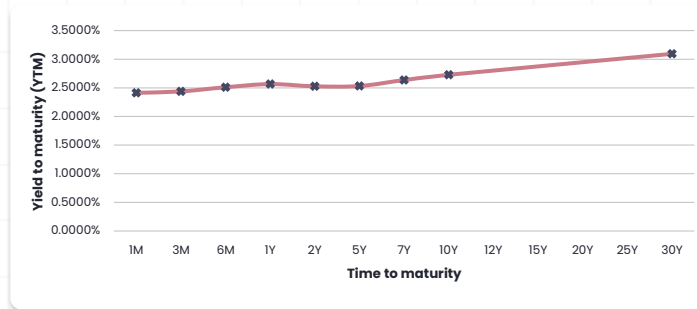
Issuers have **several bonds** with different **maturity dates outstanding**

A yield curve is a **graphical representation of bond yields at various maturities**, typically using YTM as the **yield metric**

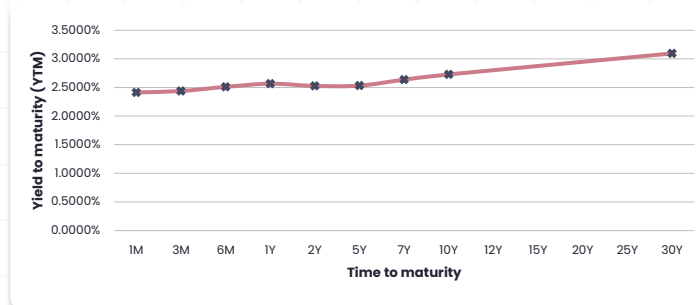
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All **bonds** used must have the same **issuer** and **credit quality**

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Credit quality refers to perceived ability of the issuer to meet **debt obligations**



U.S. government debt



Highest credit quality

U.S. Treasuries



Not mixing with bonds
from different issuers

YTM Formula

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Dirty Price (P_d)



Clean Price (P_c)

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Dirty Price (P_d)

$$P_d = \sum_{t=1}^n \frac{c_t}{(1+YTM)^t} + \frac{FV}{(1+YTM)^n}$$



The **sum** of the **present values** of all the **bonds' cash flows**, discounted using the **yield to maturity (YTM)**



Represents the **current value** of the bond



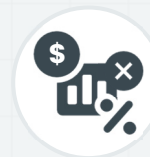
The price that **must be paid by investors** when purchasing the bond

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Dirty Price (P_d)



Accrued Interest



Clean Price (P_c)

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Accrued Interest

The interest that has **accumulated on the bond** since the **last coupon payment**, up to the purchase date of the bond



Since **coupon payments** are made at **regular intervals** (e.g., semi-annually or annually)...



...a **bondholder earns interest** over time even though they only receive **payment at the set intervals**

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Accrued Interest

The interest that has **accumulated on the bond** since the **last coupon payment**, up to the purchase date of the bond

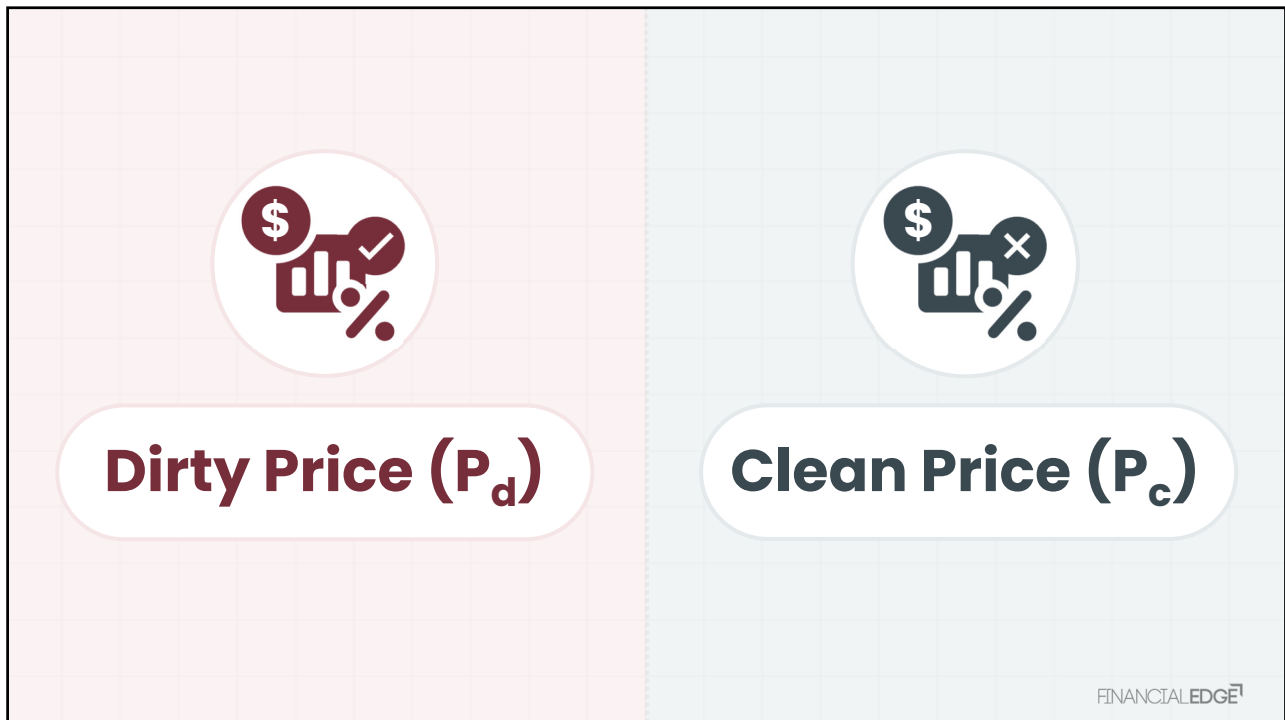


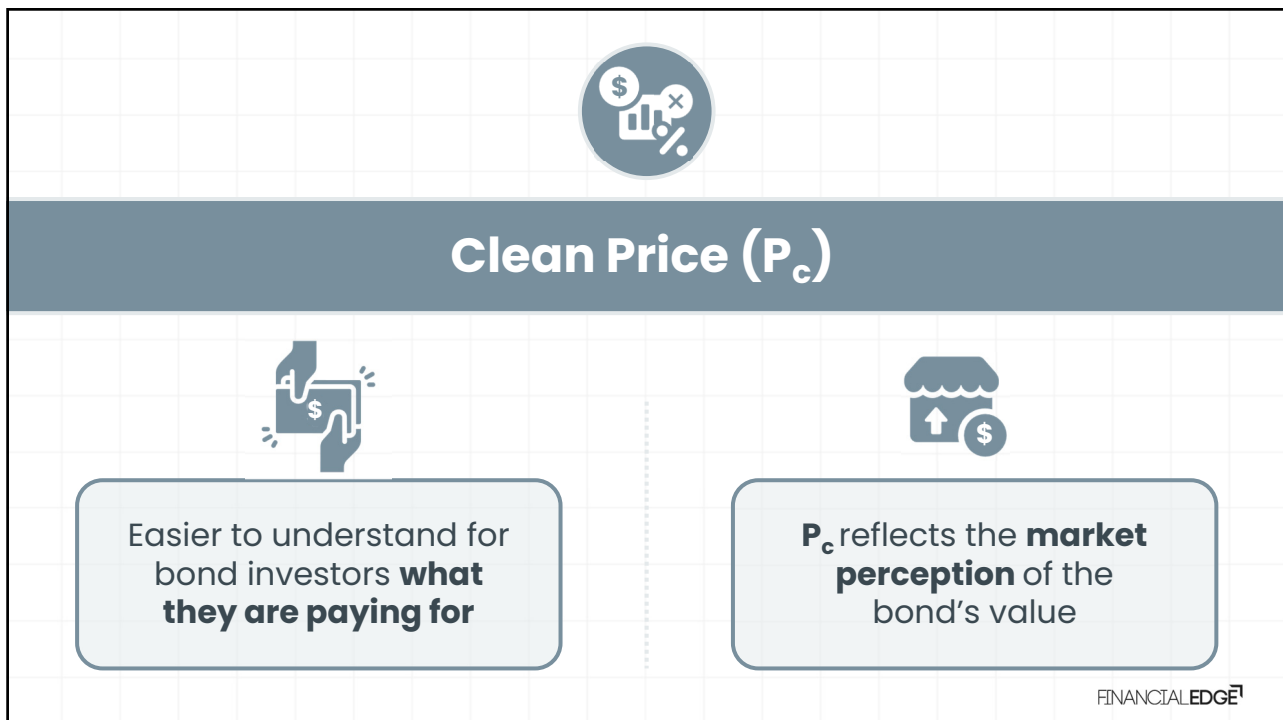
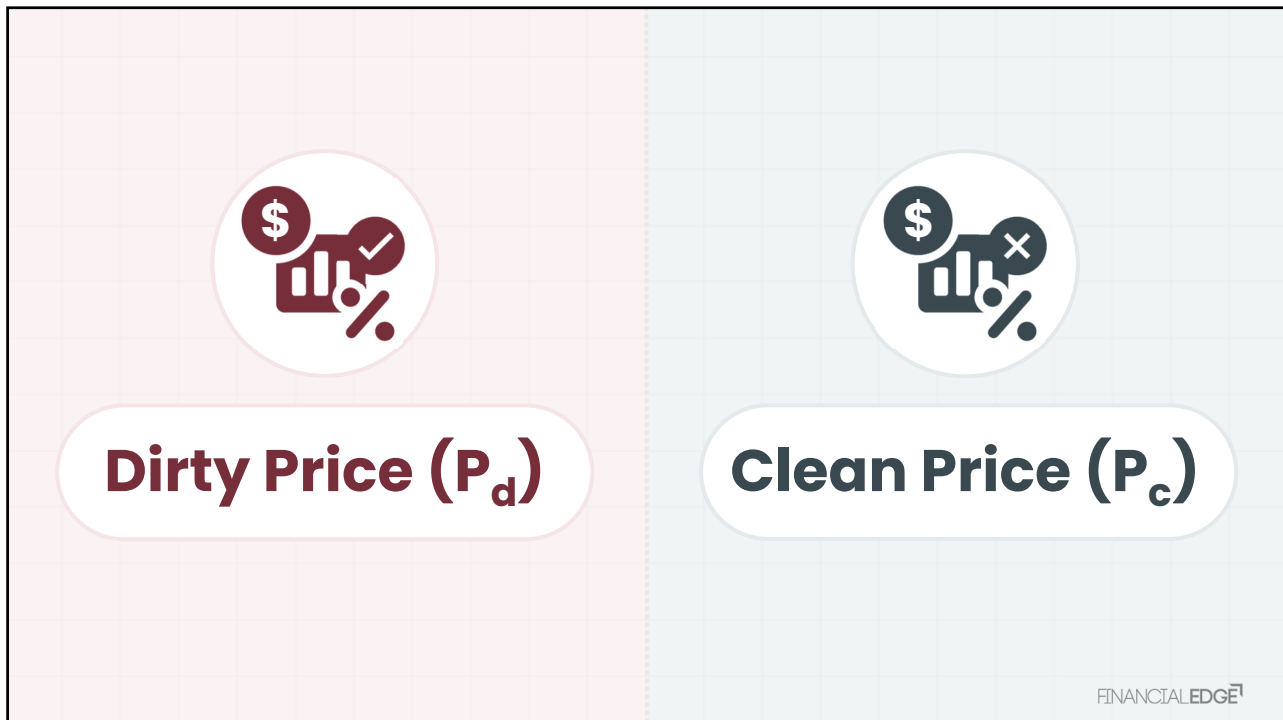
When a **bond is sold between these payment dates**...



...the **seller** is entitled to the **interest that accrued** during their ownership period

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Clean Price (P_c)



Credit risk



Interest rate risk



Time to maturity

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Dirty Price (P_d)



Clean Price (P_c)

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Dirty Price (P_d)

Bond price
changes
daily as
interest
accrues



Don't reflect
changes in bond
market valuation
or its risk and
return profile

Using clean prices, the market can **focus** on the **bond's** fundamental **value**

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Dirty vs. Clean Price

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Dirty vs. Clean Price Example

Year (t):	Cash flow:	PV:
1	2.4%	2.3431%
2	2.4%	2.2875%
3	2.4%	2.2332%
4	2.4%	2.1802%
5	102.4%	90.8164%
Total:		99.8603%

5Y bond

Annual coupon: 2.4%

YTM: 2.43%

Yield to Maturity (YTM)

Sum of PVs = P_d = 99.8603%

Present Value (PV)

Dirty Price (P_d)FINANCIALEDGE⁷

On the next business day...

Year (t):	Cash flow:	PV:
0.9973	2.4%	2.3432%
1.9973	2.4%	2.2876%
2.9973	2.4%	2.2334%
3.9973	2.4%	2.1804%
4.9973	102.4%	90.8223%
Total:		99.8669%

5Y bond one day later

Annual coupon: 2.4%

YTM: 2.43%

Yield to Maturity (YTM)

Sum of PVs = P_d = 99.8669%

Present Value (PV)

Dirty Price (P_d)FINANCIALEDGE⁷

On the next business day...

Year (t):	Cash flow:	PV:
0.9973	2.4%	2.3432%
1.9973	2.4%	2.2876%
2.9973	2.4%	2.2334%
3.9973	2.4%	2.1804%
4.9973	102.4%	90.8223%
	Total:	99.8669%

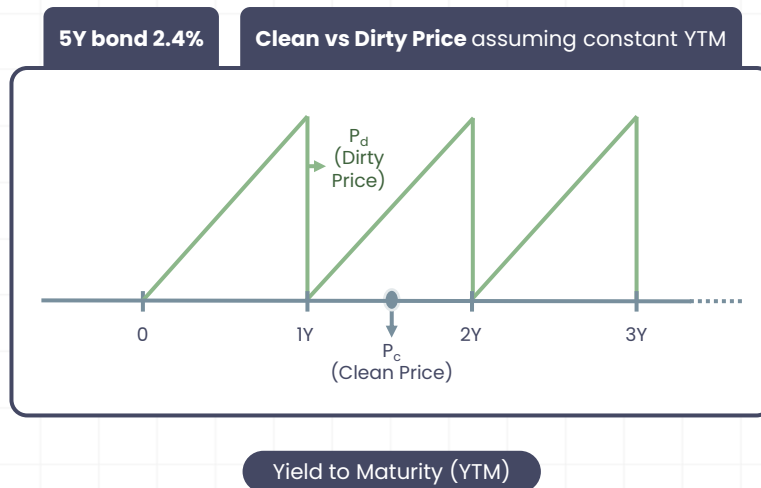
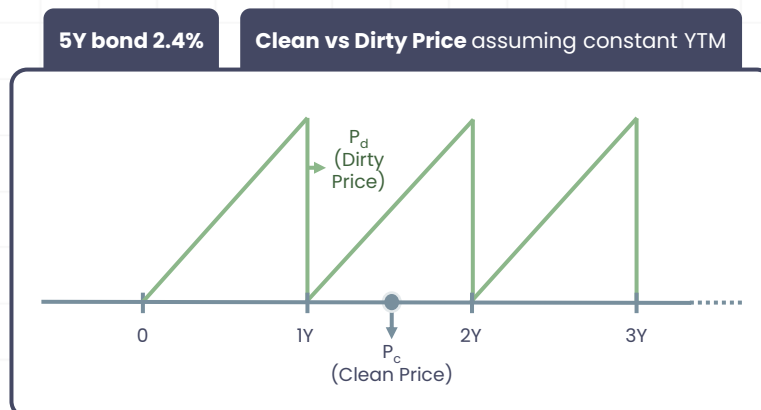
P_d includes 1 day of **accrued interest: 0.0066%**

$$2.4 \times 1/365 = 0.0066\%$$

$P_c = P_d - \text{accrued interest} = 99.8603\%$

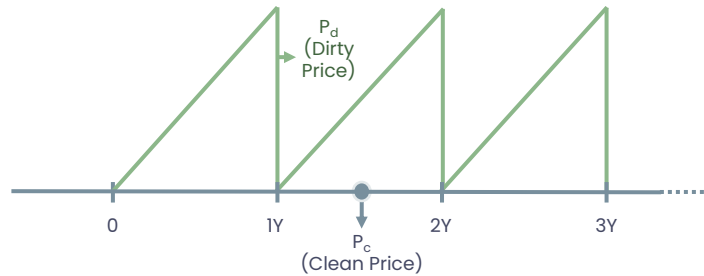
Dirty vs. Clean Price Characteristics

Assuming a **constant YTM over the life of the bond**, the development of clean and dirty prices of would compare as shown here:

FINANCIALEDGE⁷**Clean Price**Remain relatively **stable****Dirty Price**Follows a **saw tooth pattern**FINANCIALEDGE⁷

5Y bond 2.4%

Clean vs Dirty Price assuming constant YTM



Dirty Price

Increases, reflecting the
accumulation of accrued interest

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5Y bond 2.4%

Clean vs Dirty Price assuming constant YTM



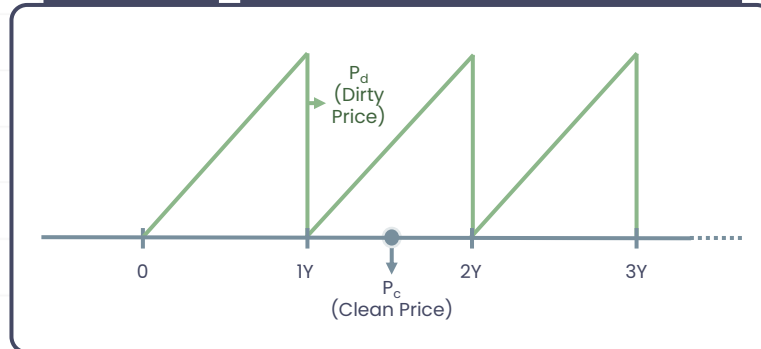
Coupon Payment Date

Bondholder receives the **coupon payment**
(includes the accrued interest)

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5Y bond 2.4%

Clean vs Dirty Price assuming constant YTM



Coupon Payment Date

The **accrued interest resets to 0**, and the dirty price **drops back down** to the level of the clean price

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Fixed Coupon Bond Cash Flow Conventions

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Bond coupons play a vital role

Investor returns



Dirty Price (P_d)



Clean Price (P_c)

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How do bond coupons work?

What happens when the payment date of a coupon falls on a weekend?

How do we divide a 365-day year into two halves for a semi-annual paying bond?

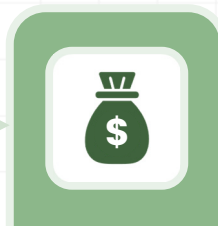
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Fixed coupon bonds are **consistent** and **constant** throughout the life of a bond



Each coupon
period



Investors receive same
amount of money

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Semi-annual payments



The bond's terms ensure that each of the **two annual coupon payments remains identical in amount**

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Cash flow example: 3.875% Treasury Mar 2025:

3 % 03/31/25 Govt		Export	Settings	Cash Flow Analysis	
99-25%/99-25%		3.985/3.979		BGN@ 10:15	
				19 Buy	10 Sell
				BBID	91282CGU9
Cash Flows		Present Values		Distressed Analysis	
Price	99-25%	Settlement	04/12/28	Issue	03/31/2023
Yield	3.978582	to	03/31/25	Maturity	03/31/2025
Amt Issd	8,458,865(M)	Amt Out	8,458,865(M)	Face Amt	1000
		Payment Date	Interest	Principal	Total
		09/30/2023	19,375.00	0.00	19,375.00
		03/31/2024	19,375.00	0.00	19,375.00
		09/30/2024	19,375.00	0.00	19,375.00
		03/31/2025	19,375.00	1,000,000.00	1,019,375.00



Investors receive two payments
of **\$19,375.00 each year**

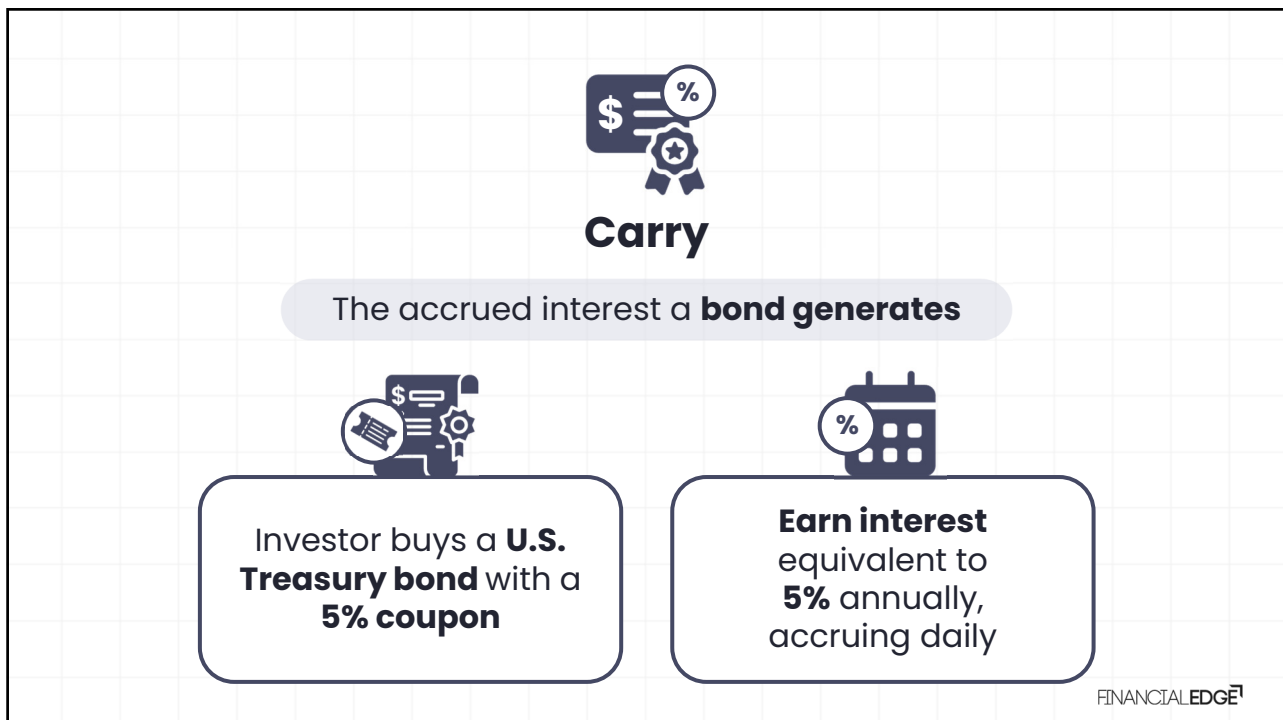
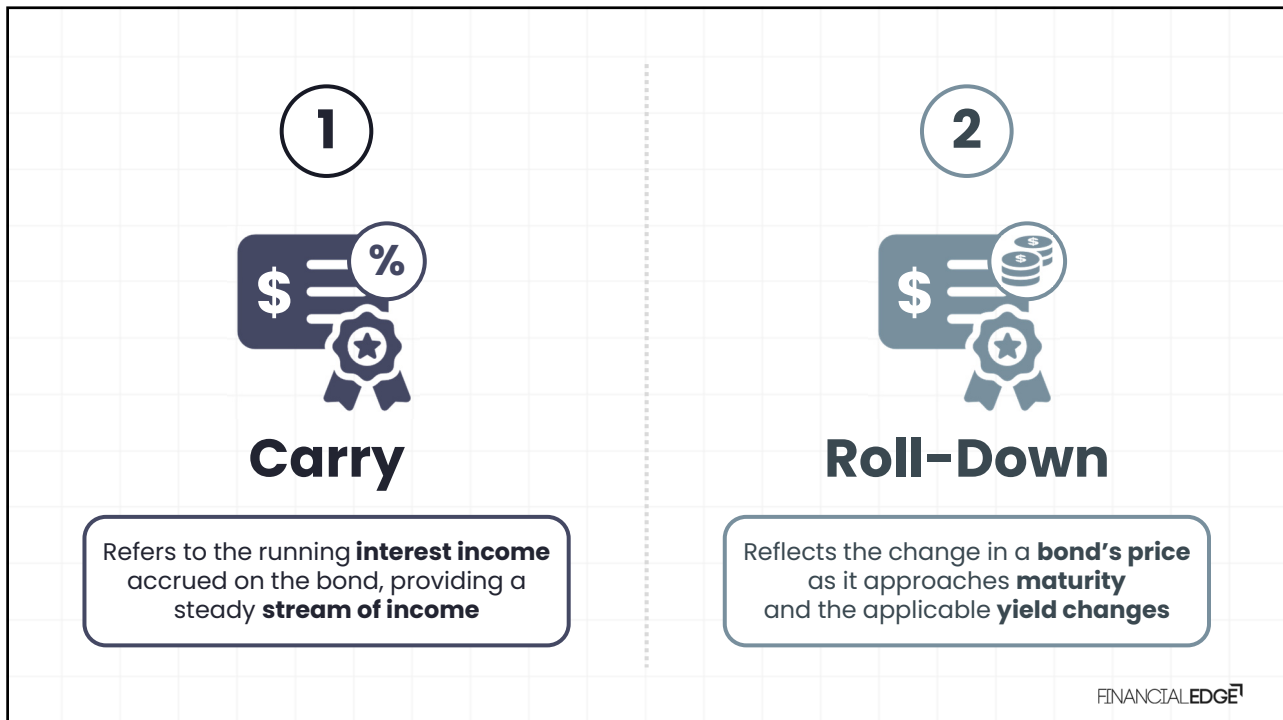


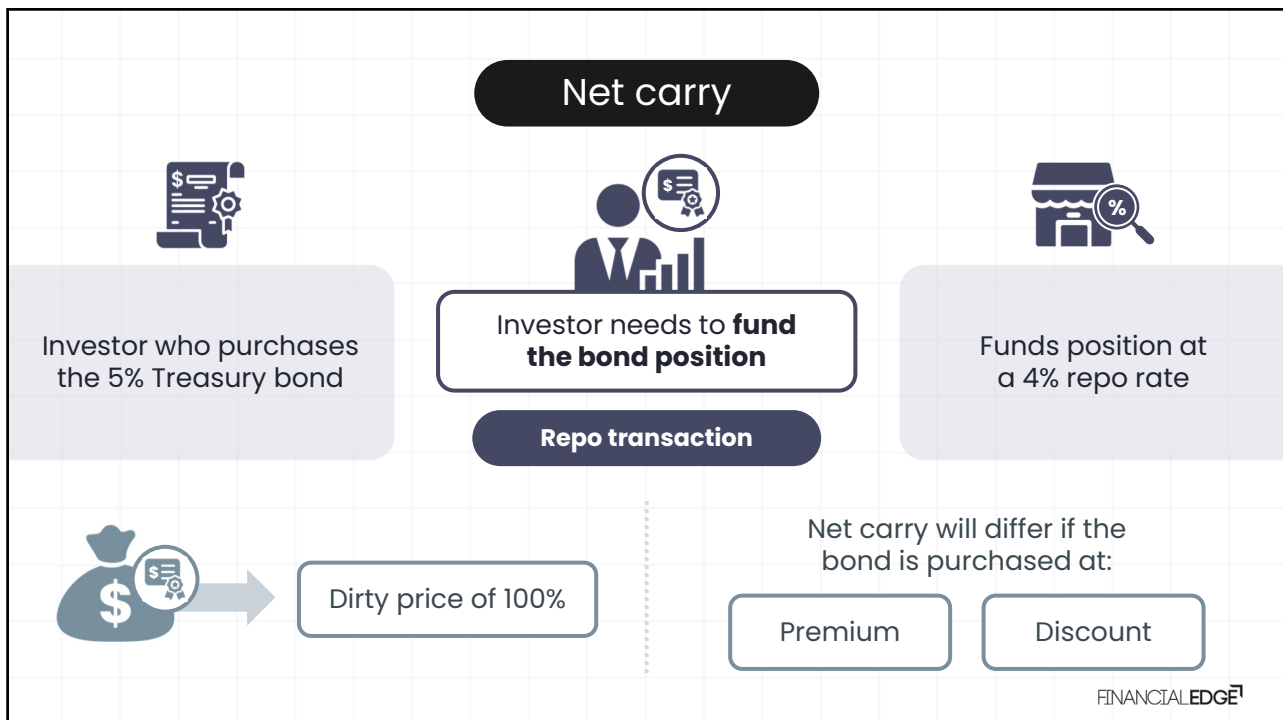
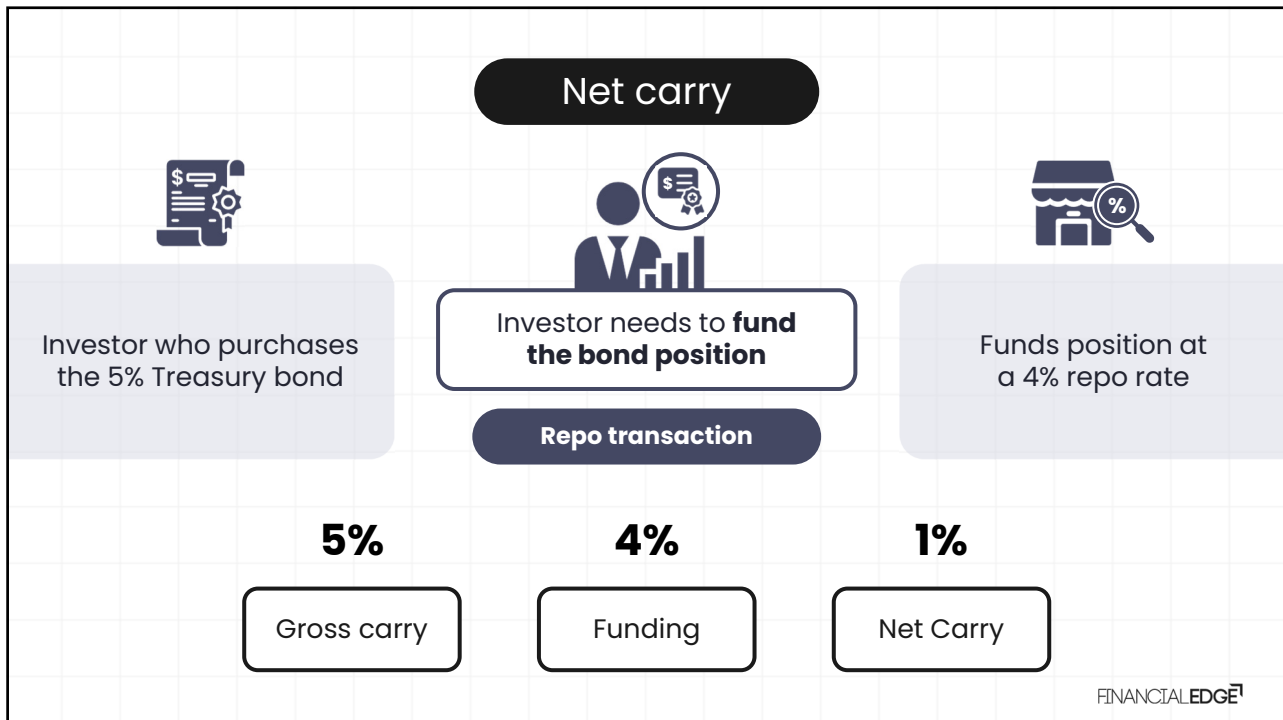
Consistency in **modeling**
and **calculations**

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Carry and Net-Carry

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Roll-Down

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1



Carry

This refers to the running **interest income** accrued on the bond, providing a steady **stream of income**

2



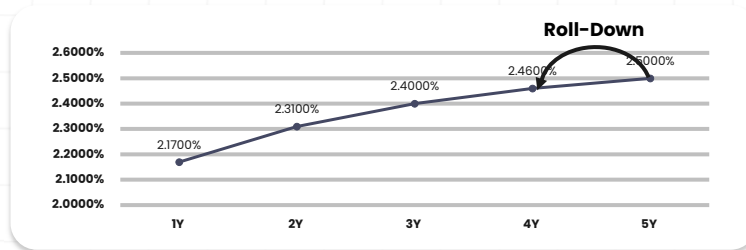
Roll-Down

This reflects the change in a **bond's price** as it approaches **maturity** and the applicable **yield changes**

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Roll-Down



In the case of a normal **upward-sloping yield curve** – a bond's price tends to **increase as it gets closer to maturity**, assuming the **yield curve remains unchanged**

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Roll-Down

Inverted Yield Curve

Short-term yields are higher than long-term yields

Roll-Down might not generate price gains but instead price declines

Roll-Down is not guaranteed income or expense

Yield curve changes – Impact how the bond's price changes

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Roll-Down

Pull-to-Par Effect

Bond's price will gradually converge toward its face value



As bond approaches its redemption date,
its clean price will **move towards par**

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